Lateral Collapse Potential of Wood Pallets by

Daniel L. Arritt
Thesis Submitted to the Faculty of the Virginia Polytechnic and State University
in partial fulfillment of the requirements for the degree of

MASTER OE SCIENCE
in
Forest Products

## APPROVED:

T.E. McLain, Chairman
M.S. White
G. Ifju

September, 1985
Blacksburg, Virginia

# Lateral Collapse Potential of Wood Pallets 

by

Daniel L. Arritt

## (Abstract)

Lateral collapse is a failure mode of wood pallets which most frequently occurs during transportation and handling. The study objective was to develop a simplified procedure for making relative comparisons in the lateral collapse potential of competing pallet designs.

A theoretical model was developed to predict the maximum horizontal force a pallet can sustain. A simple equilibrium of forces approach including joint rigidity was used. A lateral load test machine was built which induces and measures the amount of horizontal force required to collapse a pallet. After testing, the model was shown to be accurate when no upper deckboard bending occured and inaccurate when bending occured.

To account for bending, two multiple regression equations were developed to predict modification factors using a
matrix structural analysis program. A closed form solution predicts $K$-factors for two stringer designs. These $K$ factors are used to modify the resisting moments generated by the fastened joints. The modified model was shown to slightly overpredict maximum collapse load but did accurately discern differences in relative lateral collapse potential.

The ratio of the maximum horizontal load to the vertical load on the pallet provides a means of ranking the potential for lateral collapse. Those designs whose ratios fall between 0.0 and 0.6 are at high risk, from 0.6 but less then 1.0 are at medium risk, and from 1.0 to infinity are at low risk of lateral collapse. These ratios have been calibrated against documented cases of lateral collapse. The factors that influence the lateral collapse potential of a design are stringer aspect ratio, joint characteristics, unit load, and upper deck flexural rigidity.

ACKNOWLEDGEMENTS

The author wishes to extend his sincere appreciation to his committee members Drs. Thomas McLain, Marshall White, Geza Ifju, and Albert DeBonis for their leadership, advice and friendship throughout this study.

Special thanks are extended to the Cooperative Pallet Research Project funded by Va. Tech and the NWPCA for their financial support throughout this study.

Grateful acknowledgment is given to the author's employer, Timber Truss Housing Systems, Inc. of Salem, Virginia, for allowing him a leave of absence to complete this thesis.

Finally, a personal note of gratitude is extended to the author's wife, Kim, for her encouragement and sacrifices during the study, to the author's family for assisting with the basic educational opportunity and for moral support, and to Kelly Mulheren and Harold Vandivort for their invaluable assistance during this project.

TABLE OF CONTENTS
TITLE ..... PAGE

1. Introduction ..... 1
2. Literature Review ..... 4
2.1 Pallet Stability ..... 6
2.2 Joint Characteristics ..... 8
3. Theorectical Model Development ..... 17
3.1 General ..... 17
3.2 Type I Model ..... 30
3.3 Type II Model ..... 36
3.3.1 Three and Four Stringer Designs ..... 38
3.3.2 Two Stringer Design ..... 40
4. Experimental Verification ..... 46
4.1 Introduction ..... 46
4.2 Development of Lateral Load Test Machine ..... 46
4.3 Model Verification: Type I ..... 51
4.4 Model Verification: Type II ..... 61
4.5 Experimental Verification of LCAN ..... 68
5. Design Procedures and Calibration ..... 73
5.1 Introduction ..... 73
5.2 Field Survey and LCP Categories ..... 73

## TABLE OF CONTENTS (continued)

## TITLE

PAGE
5.3 Implementation into PDS-the Pallet Design System ..... 75
5.4 Documented Lateral Collapse Failures ..... 76
5.5 Variable Sensitivity ..... 77
6. Conclusions ..... 84
LITERATURE CITED ..... 86
APPENDIX A ..... 89
Al - Machine Drawings ..... 90
A2 - Machine Wiring ..... 94
A3 - Machine Operation ..... 96
A3.1 - Pre Test Calibration Procedures ..... 97
A3.2 - Typical Test Procedures ..... 98
APPENDIX B ..... 100
Bl - Listing of LCAN Program ..... 101
B2 - Analog Models ..... 118
B3 - Pallet Designs for Computer ..... 121
B3.1 - Three Stringer, Double-Faced Pallets Designed for K-Factor Development ..... 122
B3.2 - Four Stringer, Double-Faced Pallets Designed for K-Eactor Development ..... 123

## TABLE OF CONTENTS (continued)

TITLE $\quad \underline{\text { PAGE }}$
B3.3 - Three Stringer, Single-Faced Pallets Designed for K-Factor Development ..... 124
B3.4 - Four Stringer, Single-Faced Pallets Designed for K-Factor Development ..... 125
APPENDIX C ..... 126
C1 - Fastener Patterns ..... 127
C2 - Construction Specifications and Unit Load for Type I Pallets ..... 130
C3 - Construction Specifications for Joint Rotation Samples ..... 132
C3.1 - Specification of Joint Rotation Samples Fastened with Nails ..... 133
C3. 2 - Specification of Joint Rotation Samples Fastened with Staples ..... 134
C3. 3 - Specification of Joint Rotation Samples for Rate of Loading Study ..... 135
C4 - Upper Deckboard MOE by Pallet ..... 136
C5 - Construction Specifications and Unit Load for Type II Pallets ..... 140
C6 - Construction Specifications and Unit Load for Field Pallets ..... 142
APPENDIX D ..... 145
D1 - Result of Joint Rotation Tests ..... 146
D1.1 - Test Results of Joint Rotation Samples for Nails ..... 147

TABLE OF CONTENTS (continued)
TITLE ..... PAGE
D1.2 - Test Results of Joint Rotation Samples for Staples ..... 148
D1.3 - Test Results of Joint Rotation Samples for Rate of Loading Study ..... 149
D2 - Regression Equations for Individual Joints ..... 150
D2.1 - K-factor Regression Equations and Corresponding R-Square Values for 3 Stringer, Single-faced Pallets ..... 151
D2.2 - K-factor Regression Equations and Corresponding R-Square Values for 3 Stringer, Double-faced Pallets ..... 152
D2.3 - K-factor Regression Equations and Corresponding $R$-Square Values for 4 Stringer, Single-faced Pallets ..... 153
D2. 4 - K-factor Regression Equations and Corresponding R-Square Values for 4 Stringer, Double-faced Pallets ..... 154
VITA ..... 155

## List of Abbreviations

| Ar | - | aspect ratio (w/d) (in./in.) |
| :---: | :---: | :---: |
| b | - | width of upper deckboards (in.) |
| C | - | diagonal distance of stringer cross section (in.) |
| CL | - | inside distance between the legs of the staple measured at the crown (in.) |
| C | - | compression perpendicular to the grain (lbs.) |
| d | - | height of stringer (in.) |
| E | - | modulus of elasticity (psi.) |
| $E_{t}$ | - | combined E of upper deckboards (psi.) |
| FQI | - | fastener quality index |
| FWT | - | fastener withdrawal resistance (lbs.) |
| G | - | specific gravity |
| h | - | horizontal force applied to each stringer (lbs.) |
| H | - | horizontal force applied to pallet (lbs.) |
| $\mathrm{H}_{\text {eq }}$ | - | $H$ required to maintain equilibrium of SPACEPAL analog models (lbs.) |
| $\mathrm{H}_{\text {max }}$ | - | maximum $H$ a pallet can sustain before collapse (lbs. |
| $\mathrm{H}_{\text {tot }}$ | - | H applied to SPACEPAL analog models (lbs.) |
| HD | - | head diameter of nail (in.) |
| HP | - | head pull-through resistance (lbs.) |
| HX | - | number of helix per inch of thread length |
| i | - | number of a stringer |
| $I_{t}$ | - | combined moment of inertia of upper deckboards (in ${ }^{4}$ ) |

## List of Abbreviations (continued)

j - number of a deckboard
K1 - modification factor for top joint moments
K2 - modification factor for bottom joint moments
$\mathrm{K}_{3}$ - three stringer modification factor for joint moments
$K_{4}$ - four stringer modification factor for joint moments
\& - center to center distance between outer stringers (in.)
$\ell^{\prime}$ - deckboard overhang (in.)
LCP - lateral collapse potential
ml - resisting moments of individual top deckboardstringer joints (in.-lb.)
m2 - resisting moments of individual bottom deckboardstringer joints (in.-lb.)

M - moment (in.-lb.)
M1 - sum of $m 1$ (in.-1b.)
M2 - sum of m2 (in.-lb.)
$M^{s}$ - total $m 1$ from SPACEPAL analysis (in.-lb.)
M2 ${ }^{s}$ - total $m 2$ from SPACEPAL analysis (in.-lb.)
MC - moisture content (\%)
ND - total number of upper deckboards
NS - total number of stringers
P - penetration in holding member (in.)
q - upper deckboard thickness (in.)

List of Abbreviations (continued)
$r 1$ - $R$ of top deckboard-stringer joints (in.-lb./radian)
$r 2$ - $R$ of bottom deckboard-stringer joints (in.-lb./radian)

R - rotation modulus (in.-lb./radian)
R1 - sum of rl (in.-lb./radian)
R2 - sum of r2 (in.-lb./radian)
$S$ - reaction to unit load by stringers (lbs.)
T - thickness of fastened member (in.)
TH - thread-crest diameter of a nail (in.)
u - distributed unit load (lbs./in.)
V - unit load (lbs.)
w - width of stringer (in.)
WD - wire diameter (in.)
WW - diameter or width of crown (in.)
X - horizontal displacement of stringer (in.)
Y - vertical distance from assumed point of rotation to $h_{i}$ (in.)
$Z \quad-\quad$ lever-arm distance of $V$ (in.)
a - angle between $C$ and $w$ (radians)
$\alpha^{\prime} \quad-\quad$ angle between $C$ and horizontal plane at point $A$ (radians)

B1 - opening of the upper deckboard-stringer joints for a Type II, two stringer pallet (radians)

B2 - opening of the lower deckboard-stringer joints for a Type II, two stringer pallet (radians)

List of Abbreviations (continued)
© - angular rotation (radians)
$\phi 1$ - $\phi$ of upper deckboard-joint (radians)
$\phi 2$ - $\quad$ of lower deckboard-joint (radians)
$\lambda 1$ - angle between horizontal plane at point $A$ and top deckboards due to end moments (radians)
$\tau 1$ - angle between horizontal plane at point $A$ and top deckboards due to distributed load between supports (radians)
$\boldsymbol{\xi} \quad-\quad$ total angular rotation between horizontal plane at point $A$ and top deckboards due to unit load (radians)

## List of Figures

FIGURE ..... PAGE
2.1 - An Illustration of Tests which Determine Joint Properties ..... 10
2.2 - Typical Moment (in.-lb.)-Rotation (Radians) Curve from Joint Rotation Test ..... 11
2.3 - Nail Nomenclature ..... 14
2.4 - Staple Nomenclature ..... 16
3.1 - The Effect Unit Load has on a Collapsing, Type I Pallet ..... 19
3.2 - Load Distribution on a Two Stringer Pallet ..... 23
3.3 - Load Distribution on a Three Stringer Pallet ..... 24
3.4 - Load Distribution on a Eour Stringer Pallet ..... 25
3.5 - The Deckboard-Stringer Joint ..... 28
3.6 - The Effect Unit Load has on a Collapsing, Type II Pallet ..... 37
3.7 - The Effect Unit Load has on a Collapsing, Two Stringer, Type II Pallet ..... 41
3.8 - An Illustration of how $\lambda_{1}$ and $\lambda_{2}$ are Calculated Utilizing the Principles of Superposition ..... 43
4.1 - Photograph of Test Machine ..... 48
4.2 - Plan and Profile Views of Test Machine ..... 49
4.3 - Photograph of Collapse Test ..... 53
4.4 - Horizontal Eorce (lbs.) vs. Horizontal Translation (in.) Curve from Collapse Test ..... 54

List of Eigures (continued)
FIGURE ..... PAGE
4.5 - The Change in Rank of $\mathrm{H} 2_{\text {max }} / V$ Versus the $\mathrm{H}_{\text {max }} / V$ Rank for 3 Stringer Pallets ..... 66
4.6 - The Change in Rank of $\mathrm{H} 2_{\max } / \mathrm{V}$ Versus the ${ }^{H 1}$ max $/ V$ Rank for 4 Stringer Pallets ..... 67
5.1 - The Effect Stringer Aspect Ratio has on $\mathrm{H}_{\text {max }} / \mathrm{V}$ ..... 78
5.2 - The Effect Unit Load Ratio has on $H_{\text {max }} / V$ ..... 80
5.3 - The Effect of Elexural Rigidity on $H_{\max } / V$ ..... 81
5.4 - The Effect Maximum Moment of the Joints has on $H_{\text {max }} / V$ ..... 83
Al. 1 - End Profile Views of Test Machine ..... 91
Al. 2 - Plan and Profile Views of Buttress-Load Head Connection ..... 92
A1. 3 - Details of LVDT Bracket ..... 93
A2.1 - Electrical Wiring Diagram of Test Machine ..... 95
B2.1 - Three Stringer Analog Model ..... 119
B2.2 - Eour Stringer Analog Model ..... 120
C1.1 - Nail Patterns ..... 128
C1. 2 - Staple Patterns ..... 129

List of Tables
TABLE ..... PAGE
4.1 - Actual $H_{\text {max }}$ Versus Predicted $H_{\text {max }}$ for Type I Tests ..... 55
4.2 - Average $M_{\max }$ Values for Modification Factor Analysis ..... 58
4.3 - Average $R$ Values for Modification Factor Analysis ..... 59
4.4 - Actual $H_{\max }$ Versus Predicted $H_{\text {max }}$ after Reanalysis of Type I Tests ..... 60
4.5 - Actual $H_{\text {max }}$ Versus Predicted $H_{\max }$ for Type II Tests ..... 71
B3.1 - Three Stringer, Double-Faced Pallets Designed for K-Factor Development ..... 122
B3.2 - Four Stringer, Double-Faced Pallets Designed for K-Factor Development ..... 123
B3.3 - Three Stringer, Single-Faced Pallets Designed for K-Factor Development ..... 124
B3. 4 - Four Stringer, Single-Faced Pallets Designed for K-Factor Development ..... 125
C2 - Construction Specifications and Unit Load for Type I Pallets ..... 131
C3.1 - Specification of Joint Rotation Samples Eastened with Nails ..... 133
C3. 2 - Specification of Joint Rotation Samples Fastened with Staples ..... 134
C3.3 - Specification of Joint Rotation Samples for Rate of Loading Study ..... 135
C4 - Upper Deckboard MOE by Pallet ..... 137
List of Tables (continued)
TABLE ..... PAGE
C5 - Construction Specifications and Unit Load for Type II Pallets ..... 141
C6 - Construction Specifications and Unit Load for Field Pallets ..... 143
D1.1 - Test Results of Joint Rotation Samples for Nails ..... 147
D1.2 - Test Results of Joint Rotation Samples for Staples ..... 148
D1.3 - Test Results of Joint Rotation Samples for Rate of Loading Study ..... 149
D2.1 - K-factor Regression Equations and Corresponding R-Square Values for 3 Stringer, Single-faced Pallets ..... 151
D2.2 - K-factor Regression Equations and Corresponding R-Square Values for 3 Stringer, Double-faced Pallets ..... 152
D2.3 - K-factor Regression Equations and Corresponding R-Square Values for 4 Stringer, Single-faced Pallets ..... 153
D2. 4 - K-factor Regression Equations and Corresponding R-Square Values for 4 Stringer, Double-faced Pallets ..... 154

## INTRODUCTION

Pallets are an essential component of todays' materials handling industry. They offer an economical, efficacious intermediary between unitized products and the lift-truck. More than 277 million wooden pallets were manufactured in the U.S. during 1980 (15) which shows the large demand for this product.

There are currently no standard design procedures for wooden pallets which would insure a minimum level of structural performance and serviceability. As a result most pallets are designed by trial and error, experience or not at all. Because of the very competitive nature of the industry the user, the manufacturer and the pallet industry as a whole suffer because there are no uniformly recognized guidelines for establishing a minimum pallet design for a specific application. In response to this void and a major concern with product liability, Virginia Polytechnic Institute and State University, the National Wooden Pallet and Container Association, and the U.S. Eorest Service
entered into a cooperative Pallet Research Program (PRP). The objective of this program were to develop rational design procedures which will provide a means of assessing a pallet's durability and structural adequacy prior to manufacture.

One damaging failure mode of stringer pallets in service is lateral collapse. For the purpose of this study lateral collapse is defined as the overturning of all stringers in a pallet with a unit load as a result of in-plane vibration or load. This collapse may result from an impact load perpendicular to the wide face of the stringers or to the unit load itself. Collision between forklift tines and stringers commonly induces these lateral impact loads but other horizontal, in-plane forces may also contribute to this failure. Pallets may also experience collapse due to transverse vibration during transportion of palletized loads. Lateral collapse is known to occur during rail or truck shipment with inadequate dunnage.

There are relatively few well documented cases of lateral collapse available to researchers. However, within the industry it is a well known problem although one that many users do not necessarily report to manufacturers.

Unfortunately, analysis of the load or vibration required to cause collapse is a complicated dynamic problem made further complex by innumerable different pallet geometries, fasteners, unit load types and service conditions.

The materials handing industry will benefit if some relative measure of the potential of a pallet to collapse in "average" service could be made. Undoubtedly, this could be gained empirically, although the cost of doing so would be prohibitive. As a result, this study was initiated with the global objective of developing a method to estimate a relative measure of the Lateral Collapse Potential (LCP) of single- and double-faced, stringer pallets.

## CHAPTER 2

## LITERATURE REVIEW

Understanding structural collapse and its prevention is no simple task. A review of the literature is presented to help explain these topics.

During the early years of structural engineering, large building materials, such as stones and timbers were frequently used. By incorporating these large elements into their design, er.:neers were mostly concerned with instability, not strength $(23,24)$.

These massive building materials were gradually replaced and were virtually eliminated early in the nineteenth century with the advent of metals. Long, slender elements could be fashioned from metal and used to build in new geometric proportions. With these designs, new buckling and stability problems arose. In the latter part of the nineteenth century Euler's equation became popular in buckling design. Since its refinement in the early twentieth century, Euler's equation has made the analysis of
buckling less a problem than overall structural stability (7). Today, economic pressures demand buildings to be constructed with less material and in more extreme proportions which may exagerate stability problems.

The analysis of structural stability is pursued in many directions. Often the structure, the environment, and the behavior is simulated by models; however, this approach has limited practicality. Entirely theoretical analyses are useful, but rare. The most popular approach to structural analysis is semi-theoretical and empirical for example, "column curves". Quite often, all of these techniques are used in the final design (9).

Even with the most sophisticated analysis, uncertainty of the system and environment will influence design (23). It is a good engineering practice to apply a margin of safety to the analysis and the variables affecting stability. The level of safety should be in balance with other design principles: servicability, feasibility, repairability, and aesthetics (3).

In summary of the reviewed literature to this point, the stability of any structure is a function of its environment and its design $(9,23,30)$. Included in the environmental
factors are equilibrium moisture content, snow loads, wind loads, and seismic forces. Some structural factors include material quality, fasteners, and foundations (8). Pallet behavior is governed by similar criteria.

## 2. 1 Pallet Stability

Wallin et al. (28) suggests that the design of a pallet should consider both static and shock loads. Their investigations concluded that the two most important factors affecting impact strength are 1 ) the method of pallet assembly and 2) the type and quality of pallet shook. The Pallet Exchange Program (as cited by 12) recommends placing high quality shook on the periphery of a pallet to optimize its contribution to impact resistance.

The destructive vibrational forces inflicted on a structure by shock loads are resisted by damping forces (11). The damping forces come from internal friction and the friction between the structure and its support system (4). To avoid failure of pallets due to impact loads, nailed joints should not be too rigid (27). Dunmire (5) found that those pallets whose deckboards were dry and whose stringers were green during assembly were more durable against shock loads than those assembled from completely
green material. He hypothesized that as the structure dries, a large gap is formed between the deckboards and the stringers which causes greater absorption of impact energy.

In addition to horizontal impact forces, unit loads are applied to the pallet deck. A unit load is composed of materials and products that a pallet supports (19). These materials are frequently stacked individually, in boxes, or in bags. Unit loads are considered most often to be 1) uniformly distributed over the entire deck, 2) uniformly distributed over part of the deck, or 3) concentrated (6).

In summary, the loads most frequently applied to a pallet are lateral impact and unit loads. The environment of a pallet offers many types of loads that must be recognized during design to assure a semi-predictable behavior. The arrangement of materials and the quality of those materials play a significant role in structural stability.

For instance, pallet shook always exhibits variability. As a result, each pallet will behave differently in an environment. To maximize pallet durability, those stringers and deckboards that have few defects should be placed on the periphery of the structure (19,22). To assess the overall quality of the material, a grading procedure can be incorporated into the manufacturing process (19).

The typical wooden stringer manufactured in the U.S. has dimensions ranging from $1.00 \times 3.00$ to $2.00 \times 4.00$ inches (31). Gregory (7) describes the relationship between stability and geometry of rectangles and solids. He concluded that as an object's base, hinged at one corner, increases and/or its height decreases, the horizontal load applied to the top required to induce instability increases. In a pallet the stringers act similarly. For example a pallet with greater lateral strength is produced if 3 x 4 inch stringers are used instead of 2 x 4 's. Similarly, a four stringer pallet will exhibit more lateral stiffness than a three stringer pallet made with the same size stringers (22).

## $\underline{2} . \underline{2}$ Joint Characteristics

Pallet stringers and deckboards are most frequently connected by nails or staples. The rigidity of these connections is likely to be an important variable in pallet lateral behavior. Commonly used models to describe joint rigidity are translational stiffness, separation modulus, and rotation modulus. Translational stiffness measures the rigidity of a joint in lateral loading. Loferski (12) notes that the durability of a pallet under an impact load is
directly related to the lateral load carrying capacity. The separation modulus is "the ratio of the applied withdrawal force to the corresponding separation" (Eigure 2.1). This modulus is helpful in predicting beriing stiffness of a pallet (10). The third model of joint rigidity, rotation modulus, is defined by Kyokong (10) as "the ratio of the applied moment to the angular rotation", or as defined in the following equation:

$$
\begin{equation*}
R=M / \phi \tag{1}
\end{equation*}
$$

where:

$$
\begin{aligned}
& \mathrm{R}=\text { rotation modulus (in. }-1 b . / \text { radian) }, \\
& M=\text { moment (in. }-1 b . \text { ), and } \\
& \phi=\text { angular rotation (radians). }
\end{aligned}
$$

Figure 2.2 is a $M-\phi$ curve for a nailed joint. As illustrated, there are three distinct zones of interest along the curve. Zone 1 is the initial part of the curve where $M$ is a linear function of $\phi$. Conversely, Zone 2 is characterized by non-linear behavior of the joint. Zone 3 is joint failure. For the purpose of modeling the $M-\phi$ behavior the linear function which describes the secant to Zone 1 can be used until the line intersects with a horizontal line where $M=M_{\text {max }}$.


Separation
Modulus


Rotation
Modulus

FIGURE 2.1 - An Illustration of Tests which Determine


FIGURE 2.2 - TYPICAL MOMENT (IN.-LB.)-ROTATION (RADIANS) CURVE FROM JOINT ROTAT!ON TEST

Certainly there are numerous variables that affect the MФ behavior of a joint. One such variable of a nailed joint is withdrawal resistance. Both the rotation modulus and the separation modulus are dependent on this characteristic. Withdrawal resistance is a function of several variables which include specific gravity, nail diameter, depth of penetration, type of nail shank, type of nail point, thread angle, surface coatings on the nail, wood seasoning effects, and moisture content (12,32).

Wallin and Whitenack (29) have developed an equation to estimate the withdrawal resistance of nails and staples. First:

$$
\begin{equation*}
\mathrm{EWT}=222.2(\mathrm{FQI})\left(\mathrm{G}^{2.25}\right)(\mathrm{P}) /(\mathrm{MC}-3) \tag{2}
\end{equation*}
$$

where:

$$
\begin{aligned}
& \mathrm{FWT}= \text { Fastener Withdrawal Resistance (lbs.), } \\
& \mathrm{FQI}= 221.24(\mathrm{WD})+27.15(\mathrm{TD}-\mathrm{WD})(\mathrm{Hx})+1, \\
& \mathrm{WD}= \text { wire diameter (in.), } \\
& \mathrm{TH}= \text { thread-crest diameter (in.), } \\
& \mathrm{HX}= \text { number of helix per inch of thread } \\
& \mathrm{length}, \\
& \mathrm{G}= \text { specific gravity of the holding member, } \\
& \mathrm{P}= \text { penetration in holding member (in.), and } \\
& \mathrm{MC}= \text { moisture content at assembly of the } \\
& \text { holding member (\%). }
\end{aligned}
$$

Equation 2 was developed to be used for either helically threaded or plain shank nails. Figure 2.3 illustrates the characteristics of a nail.

Another characteristic of nailed joints which may affect the limits of rotation and separation moduli, is the fastener-head pull-through resistance. Those factors that effect this resistance are moisture content, specific gravity, and the thickness of the fastened member. Furthermore, the head-bearing area significantly influences this resistance.

Eor nails, head pull-through resistance is computed using the following equation from Wallin and Whitenack (29):

$$
\begin{equation*}
H P=1,250,000(H D-W D)(T)\left(G^{2.25}\right) /(M C-3) \tag{3}
\end{equation*}
$$

where:

$$
\begin{aligned}
H P= & \text { Head Pull-Through resistance (lbs.), } \\
H D= & \text { head diameter (in.), } \\
T= & \text { thickness of fastened member (in.), } \\
G= & \text { specific gravity of fastened member, and } \\
M C= & \text { moisture content of fastened member at } \\
& \text { assembly (\%). }
\end{aligned}
$$



FIGURE 2.3-Nail Nomenclature

For staples, HP is computed as:

$$
\begin{equation*}
\mathrm{HP}=1,591,550(\mathrm{CL})(\mathrm{WW})(\mathrm{T})\left(\mathrm{G}^{2.25}\right) /(\mathrm{MC}-3) \tag{4}
\end{equation*}
$$

where:

$$
\begin{aligned}
C L= & \text { inside distance between the legs of the } \\
& \text { staple measured at the crown (in.) and } \\
W W= & \text { diameter or width of the crown (in.). }
\end{aligned}
$$

Figure 2.4 illustrates the characteristics of a staple.


FIGURE 2.4-Staple Nomenclature

## CHAPTER 3

## THEORETICAL MODEL DEVELOPMENT

3.1 General

The lateral collapse of a wood pallet is essentially a complex dynamic problem subject to many variables. Solution of this problem will require a great deal of effort and many limiting assumptions concerning the nature of the dynamic horizontal forces and/or displacements. Because of these limitations and a percieved high cost-to-benefit ratio of the necessary research for the pallet industry it seems reasonable to explore some very simplified approaches. It is understood that in taking this path any end result may lack general applicability. Nevertheless, a reasonable first step must be taken.

The underlying premise of this research is to make comparisons of stability between pallet designs and some "yardstick" or acceptance criteria. The mechanism for making this relative comparison should be sensitive to the
same variables that influence the dynamic forces causing instability. By making relative comparisons the potential problems with lateral collapse for a certain pallet design can be assessed. This technique can not identify whether a pallet will collapse under any given situation.

One simplified approach for a relative comparison is to consider a horizontal force (H) applied to a pallet in the plane of the top deckboards. This pallet may have stringers (rectangular solid elements) of varying widths but not varying height. A unit load exerts some uniformly distributed force over the top deckboard. A bottom deck may or may not be present. If $H$ is great enough, then the top deck will translate causing the stringer to rotate as in Figure 3.1. After some critical amount of rotation, the pallet will collapse.

Two approaches to this stability problem come to mind immediately. The first is a prediction of the energy required to cause the pallet stringers to rotate 90 degrees to the fully collapsed position. The second approach is to predict a maximum horizontal force ( $H_{\max }$ ) that will cause the stringer to rotate to a position of unstable equilibrium. That is, to a point where the unit load by itself will complete stringer collapse.


FIGURE 3.1 - The Effect Unit Load has on a Collapsing, Type I Pallet

Both approaches require simplifing assumptions concerning the geometry of failure, joint properties past the "elastic" range and the horizontal force which is a function of displacement. A clear selection of one approach over the other is not obvious to the author. However, a mitigating factor is that the procedure must be simple and must make sense when explained and used by users and manufacturers in the pallet industry. Since this group is relatively inexperienced in engineering science and the process of design, the procedure must be simple to be "solid". If the procedure is not accepted by this group, then all will have been for naught. For this reason the maximum horizontal force approach was selected as the most likely candidate.

The ratio of $H_{\max }$ to the vertical unit load (V) a pallet can sustain provides a convenient, unitless means of comparing the lateral behavior of pallets. The boundaries of $H_{\max } / V$ are zero and infinity. A pallet with a $H_{\max } / V$ ratio equal to zero, requires very little horizontal load to cause collapse. Conversely, the pallet which has a $H_{\max } / V$ ratio of infinity simply will not collapse.

This ratio, $H_{\max } / V$, incorporates the unit load because comparison without this value is meaningless. To illustrate
this, compare two pallet designs using $H_{\max }$ alone as the governing criteria. If design $\# 1$ has an $H_{\max }$ of $8,000 \mathrm{lbs}$. and design \#2 has an $H_{\text {max }}$ of 6,000 lbs., one is likely to conclude that design \#1 has greater resistance to lateral collapse. On the other hand, if design \#1 is known to support 5,000 lbs. and design \#2 supports 1,000 lbs., the $H_{\text {max }} / V$ ratios for design $\# 1$ and $\# 2$ are 1.6 and 6 , respectively. Utilizing the boundary conditions stated in the previous paragraph one concludes that design \#2 is the least likely of the two designs to experience lateral collapse. This ratio can only be used as a relative, not an absolute comparison. It may well be that under some conditions both designs may collapse. To help explain the design approach, the following paragraphs describe the assumptions involved in the collapse model derivation.

First, the horizontal load applied to the pallet during collapse is considered to be applied at the lower edge of the top deckboards and perpendicular to the length of the stringers (Figure 3.1). This assumption was made so that the model would recognize various deckboard thicknesses and stringer heights. It is also assumed that the unit load does not slip on the top deckboard but maintains its relative placement.

Another assumption made was that the unit load on the pallet is transmitted to the stringers in certain percentages. The load on each stringer is designated as $V_{i}$ where $i=1$ to the number of stringers. The $V_{i} s$ in the model are considered to act in a vertical direction on the corners of each deckboard-stringer joint. Thus, reactions $S_{i}$ where $i=1$ to the number of stringers are created at the stringers to support $V$. For example Figure 3.2 shows $S_{1}$ and $S_{2}$ of a two stringer pallet equals $50 \%$ of $V$. For the three and four stringer pallets (Figures 3.3 and 3.4) equations are given which are used to compute the reactions. For example, if a 3 stringer pallet that had 48" deckboards, where $\ell^{\prime}=4^{\prime \prime}$ and $\ell=40^{\prime \prime}$, and $V=1000 \mathrm{lbs}$. , then $S_{1}=S_{3}=292$ lbs. and $S_{2}=708$ lbs.

The slight rounding of the stringer's edges that occurs during collapse because of the compression perpendicular to grain ( $C_{\perp 1}$ ) of wood is not recognized in the model. This assumption was made because the extreme variability of $C_{\mu}$ among species would have made it extremely difficult to account for in the model. Furthermore, the rounding effect results in only a small change in the location of $V_{i}$ that the overall effect on $H_{\max }$ is negligible.


$$
S_{1}=S_{2}=\frac{V}{2}
$$

FIGURE 3.2 - Load Distribution on a Two Stringer Pallet


$$
\begin{aligned}
& S_{1}=S_{3}=(V)\left(\frac{L^{\prime}+2 / 4}{2 l^{\prime}+2}\right) \\
& S_{2}=(V)\left(\frac{l / 2}{2 l^{\prime}+l}\right)
\end{aligned}
$$

FIGURE 3.3 - Load Distribution on a Three Stringer Pallet


$$
\begin{aligned}
& \ell \frac{\Delta}{S_{1}} \quad l_{2} \quad S_{2} \quad l_{1} \quad S_{3} l_{2} \quad S_{4} l^{\prime} \\
& S_{1}=S_{4}=(V)\left(\frac{l^{\prime}+l_{2} /^{\prime} 2}{2 l^{\prime}+2 l_{2}-l_{1}}\right) \\
& S_{2}=S_{3}=(V)\left(\frac{l_{1} / 2+l_{2} / 2}{2 l^{\prime}+2 l_{2}+l_{1}}\right)
\end{aligned}
$$

FIGURE 3.4 - Load Distribution on a Four Stringer Pallet

The assumptions presented have dealt with the external forces that may act on a pallet. An internal characteristic considered is the nailed or stapled deckboard-stringer joints which causes resisting moments to collapse as a horizontal force is applied. These moments are denoted by $m_{i j}$ where $i=1$ to the number of stringers (NS) and $j=1$ to the number of deckboards (ND) along each stringer. The value of each moment is a function of all the material and geometric parameters as well as the amount of rotation the joints experience. For example, if there are six upper deckboards on a pallet, then $m_{i 1}, \ldots m_{i 6}$ resisting moments occur along each stringer. Summation of these moments yields the total resisting moments for each stringer. The total moment for the top joints are denoted by $M 1_{i}=\sum_{j=1}^{N D} m 1_{i j}$. And the total bottom moment is $M 2_{i}=\sum_{j=1}^{N D} m 2_{i j}$.

Additionally, define a weighted average of the upper deckboards' moduli of elasticity as:

$$
\begin{equation*}
\left.E_{t}=\frac{1}{\sum_{j=1}^{N D b_{j}}} \sum_{j=1}^{N D}\left(b_{j}\right)\left(E_{j}\right)\right) \tag{5}
\end{equation*}
$$

where:

$$
\begin{aligned}
E_{t}= & \text { combined modulus of elasticity of upper } \\
& \text { deckboards (psi), } \\
b_{j}= & \text { width of the } j^{t h} \text { upper deckboard (in.), }
\end{aligned}
$$

$$
\begin{aligned}
E_{j}= & \text { modulus of elasticity of } j^{\text {th }} \text { upper } \\
& \text { deckboard (psi), and } \\
N D= & \text { number of upper deckboards. }
\end{aligned}
$$

Similarly, the moment of inertia of the upper deckboards is calculated as:

$$
\begin{equation*}
I_{t}=\left(q^{3} \sum_{j=1}^{N D} b_{j}\right) / 12 \tag{6}
\end{equation*}
$$

where:

$$
\begin{aligned}
I_{t}= & \text { combined moment of inertia of upper } \\
& \text { deckboards (in. }{ }^{4} \text { ) and } \\
q= & \text { upper deckboard thickness (in.). }
\end{aligned}
$$

A typical pallet deckboard-stringer joint is modeled as shown in Figure 3.5 where:

$$
\begin{aligned}
\mathrm{X}_{\mathrm{i}}= & \text { horizontal displacement of point } A \text { on } \\
& \text { stringer } i \text { (in.) from initial rest position, } \\
Y_{i}= & \text { vertical distance from assumed point of } \\
& \text { rotation (o) to } h_{i} \text { on stringer } i \text { (in.), } \\
\mathrm{V}_{\mathrm{i}}= & \text { vertical load assumed to be transmitted to } \\
& \text { stringer } i(l b s .) \text { at point } A, \\
\mathrm{~h}_{\mathrm{i}}= & \text { horizontal disturbing force on stringer } i \\
& (\text { lbs.), } \\
\mathrm{d}_{\mathrm{i}}= & \text { height of stringer } i \text { (in.), } \\
\mathrm{w}_{\mathrm{i}}= & \text { width of stringer } i \text { (in.), } \\
\phi 1_{i}= & \text { angular opening of upper deckboard-stringer } i \\
& j o i n t \text { (radians), }
\end{aligned}
$$



FIGURE 3.5 - The Deckboard-Stringer Joint

$$
\begin{aligned}
\phi 2_{i}= & \text { angular opening of lower deckboard-stringer } \mathrm{i} \\
& \text { joint (radians), } \\
\mathrm{M} 1_{\mathrm{i}}= & \text { sum of the resisting moments from the } \\
& \text { joints along the top of stringer } \mathrm{i} \\
& (i n .-1 b . / \text { radian), and } \\
\mathrm{M} 2_{\mathrm{i}}= & \text { sum of the resisting moments from the } \\
& \text { joints along the top of stringer } \mathrm{i} \\
& (\text { in. }-\mathrm{lb} . / \text { radian). }
\end{aligned}
$$

Finally, a very important criterion is the interrelationship between $E_{t} I_{t} / 1^{3}$ (l=distance between stringers) of the upper deckboards and the unit load on the pallet. Each plays a significant role in the amount of bending of the upper deckboards. For this study two pallet responses are recognized: Type $I$ where negligible bending occurs in the top deck and Type II where the upper deckboards significantly bend under load. The reason bending plays a role in lateral collapse is that it influences joint behavior during collapse. When no bending occurs in the upper-deckboards each joint has the same amount of rotation for a given top deck translation. Therefore, by using the M- $\phi$ curve all joint $m_{i j}$ 's can be determined and solving for $\mathrm{H}_{\text {max }}$ is a linear problem.

On the otherhand, deckboard bending during collapse causes the joints to open by unequal amounts. As a result, the moment generated in each joint is different making the determination of $H_{\max }$ a complex non-linear problem.

## 3. 2 Type I Model

Type I pallets experience no bending in the upper deckboards; therefore, the angular rotation, $\phi 1_{i}$ and $\phi 2_{i}$, are equal. This is true for two, three, and four stringer pallets. It is the purpose of this section to present the theory used to develop the model which predicts $H_{\max }$ for the Type I pallet.

The model is based on stability concepts described by Gregory (7). Consider the diagram of an individual stringer as illustrated in Eigure 3.5, after some significant rotation has occurred. Summing moments about point $\circ$ yields:

$$
\begin{equation*}
\Sigma M_{0}=0=h_{i}\left(Y_{i}\right)-V_{i}\left(w_{i}-X_{i}\right)-M 1_{i}-M 2_{i} \tag{7}
\end{equation*}
$$

Rearranging equation (7) gives:

$$
\begin{equation*}
h_{i}=\left(V_{i}\left(w_{i}-X_{i}\right)+M 1_{i}+M 2_{i}\right) / Y_{i} \tag{8}
\end{equation*}
$$

Before using equation (8) to calculate $H_{\max }$ an explanation of each variable is in order..

In Figure 3.5, $V_{i}$ is located on the uppermost corner of the stringer and has a leverarm distance $\left(Z_{i}\right)$ with respect to point o:

$$
\begin{equation*}
z_{i}=w_{i}-x_{i} \tag{9}
\end{equation*}
$$

As the force $h_{i}$ is applied to the structure its lever-arm distance, $Y_{i}$, increases (Eigure 3.5). This is true until $Y_{i}$ $=C_{i}$ where:

$$
\begin{equation*}
c_{i}=\sqrt{d_{i}^{2}+w_{i}^{2}} \tag{10}
\end{equation*}
$$

where:

$$
\begin{aligned}
C_{i}= & \text { diagonal distance of stringer i cross-section } \\
& \text { (in.). }
\end{aligned}
$$

Since $Z_{i}$ and $C_{i}$ are known, the lever-arm distance of $h_{i}$ is:

$$
\begin{equation*}
Y_{i}=\sqrt{C_{i}^{2}-z_{i}^{2}} \tag{11}
\end{equation*}
$$

where:

$$
Y_{i}=\text { lever-arm distance of } h_{i} \text { (in.). }
$$

At this point all external rotational moments acting on a pallet can be evaluated by multiplying force times lever-arm distance. A method to calculate the internal resistance to collapse was required to complete the model.

During collapse the resisting moments $\mathrm{Ml}_{\mathrm{i}}$ and $\mathrm{M} 2_{i}$ are generated by the fasteners used to hold the joints together. As explained in Chapter 2 the resisting moment of a joint can be described by the $M-\phi$ curve (Figure 2.2). For simplification, the joint rotation is assumed to be perfectly elasto-plastic with the secant to Zone 1 as the linear initial portion of the curve. To calculate $\mathrm{Ml}_{\mathrm{i}}$ and M2 ${ }_{i}$, $\phi$ must be computed in the following mannar:

$$
\begin{equation*}
\alpha_{i}=\tan ^{-1}\left(d_{i} / w_{i}\right) \tag{12}
\end{equation*}
$$

where:

$$
\alpha_{i}=\text { angle between } C_{i} \text { and } w_{i} \text { (radians). }
$$

And:

$$
\begin{equation*}
\alpha_{i}^{\prime}=\sin ^{-1}\left(Y_{i} / C_{i}\right) \tag{13}
\end{equation*}
$$

where:

$$
\begin{aligned}
\alpha_{i} & =\text { angle between } C_{i} \text { and the horizontal plane at } \\
& \text { point } A \text { (radians). }
\end{aligned}
$$

The angle through which the bottom joints rotate is then:

$$
\begin{equation*}
\phi 2_{i}=\alpha_{i}^{\prime}-\alpha_{i} \tag{14}
\end{equation*}
$$

where:

$$
\begin{aligned}
\phi 2_{i}= & \text { angular opening of lower deckboard-i } \\
& \text { stringer joint (radians). }
\end{aligned}
$$

Because of the definition of the Type $I$ response it is known that $\phi 1_{i}=\phi 2_{i}$. Thus:

$$
\begin{equation*}
M 1_{i}=\left(\phi 1_{i}\right)\left(R 1_{i}\right) \tag{15}
\end{equation*}
$$

where:

$$
\begin{aligned}
\mathrm{MI}_{i}= & \text { sum of the resisting moments from the } \\
& \text { joints along the top of stringer } i \\
& \text { (in.-lb.), } \\
R 1_{i}= & \text { sum of rotational moduli of top deckboard- } \\
& i^{\text {th }} \text { joints (in.-lb./radian). }
\end{aligned}
$$

Similarly:

$$
\begin{equation*}
M 2_{i}=\left(\phi 2_{i}\right)\left(R 2_{i}\right) \tag{16}
\end{equation*}
$$

where:

$$
\begin{aligned}
\mathrm{M} 2_{i}= & \text { sum of the resisting moments from the } \\
& \text { joints along the bottom of the stringer } i \\
& (i n .-l b .) \text { and } \\
R 2_{i}= & \text { sum of rotational moduli of bottom deck- } \\
& \text { board- }{ }^{\text {th }} \text { stringer joints (in.-lb./radian). }
\end{aligned}
$$

Equations (15) and (16) are misleading by implying that as long as $\phi$ increases, so does $M$. The results of actual joint tests show that $M$ does increase up to a maximum $M_{\text {max }}$. $M_{i, \max }$ and M2 $i_{i, \max }$ are computed with:

$$
\begin{align*}
& M 1_{i, \max }=\sum_{j=1}^{N D} m 1_{i j, \max }  \tag{17}\\
& M 2_{i, \max }=\sum_{j=1}^{N D} m 2_{i j, \max } \tag{18}
\end{align*}
$$

where:

$$
\begin{aligned}
M 1_{i, \max } ; \mathrm{M} 2_{i, \max }= & \text { sum of maximum moments of } \\
& \text { joints along top or bottom } \\
& \text { of stringer } i \text { (in. }-1 b . \text { ) and } \\
\mathrm{m} 1_{i j, \max } ; \mathrm{m} 2_{i j, \max }= & \text { maximum moments of } \\
& \text { individual joints along top } \\
& \text { or bottom of stringer i } \\
& (i n .-1 b .) .
\end{aligned}
$$

The $R 1_{i}$ and $R 2_{i}$ used in equation (15) and (16) are the sums of the rotational moduli along each stringer where:

$$
\begin{equation*}
R 1_{i}=\sum_{j=1}^{N D} r m 1_{i j} \quad R 2_{i}=\sum_{j=1}^{N D} r m 2_{i j} \tag{19;20}
\end{equation*}
$$

where:

$$
\begin{aligned}
& R 1_{i} ; R 2_{i}=\text { sum of rotational moduli of the } \\
& \text { joints along the top or bottom of } \\
& r m 1_{i j} ; r m 2_{i j}=\text { rotational moduli of individual } \\
& \text { deckboard-stringer joint along top } \\
& \text { or bottom of stringer } \\
& \text { (in.-lb./radian). }
\end{aligned}
$$

Knowing the joint moments as a function of rotation (or horizontal displacement, $X$ ) it is possible to solve equation (8) for $h_{i}$. However, the computed $h_{i}$ is only the amount of force necessary to cause an amount of displacement in stringer i. The total horizontal force necessary to cause the total amount of displacement is found using:

$$
\begin{equation*}
H=\sum_{i=1}^{N S} h_{i} \tag{21}
\end{equation*}
$$

The $H_{\text {max }}$ a pallet can sustain is determined by incrementing $X$ until $H$ is maximized. Generally, $H_{\max }$ occurs before $X=2$ inches in actual tests of typical pallets. To help minimize the error in estimating $H_{\max }$ the size of the increments of $X$ should not exceed 0.1 inch.

In summary, the solution to finding the $H_{\max }$ for a Type I pallet is as follows:

1. determine the load distributed to each stringer ( $\mathrm{V}_{\mathrm{i}}$ ),
2. determine the constants which describe each joint type ( $R_{i j}$ and $M_{i j, \max }$ ),
3. introduce a small horizontal displacement (X),
4. determine $M 1_{i}$ and $M 2_{i}$ for each stringer by summing the proper $m_{i j}$ 's,
5. compute $h_{i}$ for each stringer using equation (8),
6. sum the $h_{i}^{\prime}$ 's (equation 21) to give the total $H$ at that increment, and
7. repeat steps three through six until $H$ is maximized ( $H_{\text {max }}$ ).

## 3. 3 Type II Model

Type II pallets experience upper deckboard deflection during collapse, and therefore, $\phi 1_{i} \neq \phi 2_{i}$. Figure 3.6 shows that bending of the top deckboard cause the stringers to experience different amounts of horizontal translations due to geometric non-linearity. Since each stringer may translate differently, $\phi 1_{i} \neq \phi 2_{i}$.

As a result of this non-linearity, the moments generated in the joints during collapse are not equal as they are in the Type I pallet; therefore, the moments in equation (8) must be modified. Another possibility is that the deckboards will behave as combined bending and axial force members and may buckle. For pallets with very low top deck flexural stiffness, $E_{t} I_{t}$, this mechanism may predominate over a reduced joint moment contribution. However the end fixity conditions are typically more rigid than pins and are not easily determined. Since a beam column analysis approach would add greatly to the complexity of the solution


FIGURE 3.6 - The Effect Unit Load has on a Collapsing, Type II Pallet
with no readilly identifiable significant benefit, it was not persued. The experimental results of a wide variety of pallets and sections failed to demonstrate a significant combined bending - axial force influence on collapse. However, this does not mean that this mode could not be prevail in some circumstances.

### 3.3.1 Three and Four Stringer Designs

The purpose of this section is to describe how the modification factors for the joint moments in three and four stringer pallets were developed for the Type II model. Physically testing the influence of unit loads, stringer dimensions, deckboard properties, and nail properties on lateral collapse in this mode would be immensely time consuming and expensive. This testing was reduced by utilizing a computer program, SPACEPAL (17), which is capable of analyzing structures using the stiffness method of matrix structural analyses. SPACEPAL was used to model a wide variety of pallet designs subjected to various horizontal and unit loads. The resulting theoretical top and bottom moments along each stringer ( $\mathrm{M1}^{\mathrm{S}}{ }_{i}$ and $\mathrm{M}_{2}{ }^{\mathrm{s}}{ }_{i}$ ) were evaluated. These analyses are described in Chapter 4.

If $\mathrm{M1}^{\mathrm{S}}{ }_{i}$ and $\mathrm{M}^{\mathrm{S}}{ }_{i}$ from SPACEPAL tests which accounts for Type II behavior and $\mathrm{M1}_{\mathrm{i}}$ and $\mathrm{M}_{\mathrm{i}}$ from the Type I model are known, then a modification factor can be computed for each joint of all test pallets using:

$$
\begin{equation*}
K 1_{i}=\frac{\mathrm{M1}_{\mathrm{i}}{ }^{\mathrm{S}}}{\mathrm{M} 1_{i}} \quad ; \quad \mathrm{K} 2_{i}=\frac{\mathrm{M} 2_{i}^{s}}{\mathrm{M} 2_{i}} \tag{22;23}
\end{equation*}
$$

where:

$$
\begin{aligned}
& K 1_{i} ; K 2_{i}=\operatorname{modification} \text { factors for top } \\
& \text { and bottom joint moments, } \\
& M 1_{i}{ }_{i} ; M_{i}^{s}=\text { upper and lower deckboard-stringer } \\
& \text { moments resulting from SPACEPAL } \\
& \text { analysis on pallets (in.-lb./radian) } \\
& \text { and } \\
& M 1_{i} \text {; } M 2_{i}=\text { moments from equations } \\
& \text { (15) and (16). }
\end{aligned}
$$


#### Abstract

$K 1_{i}$ and $K 2_{i}$ values were computed for a wide variety of different types of pallets. Multiple regression relationships were then developed to estimate $\mathrm{K}_{\mathrm{i}}$ and $\mathrm{K}_{\mathrm{i}}$ utilizing unit loads, stringer dimensions, deckboard dimensions, deckboard MOE's, and fastener properties as the variables. These estimated $K$-factors are multiplied by the moments determined in a Type $I$ analysis ( $\mathrm{M1}_{\mathrm{i}}$ or $\mathrm{M}_{\mathrm{i}}$ ) and the product is an estimate of the moments in a Type I pallet. One constraint imposed on the $K$-factors was that they fall


in a range $0<K$-factor $<1$. This assumes that the moment is not less than zero or greater than $M_{\text {max }}$. Therefore, if $K>1$, then $K=1$ or if $K<0$, then $K=0$.

Equation (8) for $h_{i}$ now becomes:

$$
\begin{equation*}
h_{i}=\frac{V_{i}\left(w_{i}-X_{i}\right)+K 1_{i}\left(M 1_{i}\right)+K 2_{i}\left(M 2_{i}\right)}{Y_{i}} \tag{24}
\end{equation*}
$$

### 3.3.2 Two Stringer Design

The relative simplicity of the two stringer pallet allowed the development of a closed form solution to compute $K 1_{i}$ and $K 2_{i}$. Utilizing the principle of superposition the actual structure (Figure 3.7) was modeled as both a simply supported beam with a uniform load and a simply supported beam with end moments.

In Figure 3.7, $\tau I_{1}$ and $\tau I_{2}$ are computed with:

$$
\begin{equation*}
{ }^{\tau I_{1}}=\frac{(-u)(1)}{24\left(E_{t}\right)\left(I_{t}\right)} ;{ }^{\tau I_{2}}=\frac{(u)(1)}{24\left(E_{t}\right)\left(I_{t}\right)} \tag{25;26}
\end{equation*}
$$


$+$


PARTIAL V $\left.\begin{array}{c}1 \\ \text { 2.2. }\end{array}\right]$


FIGURE 3.7 - The Effect Unit Load has on a Collapsing, Two-Stringer, Type II Pallet
where:

$$
\begin{aligned}
\tau 1_{1} ; \quad & \tau 1_{2}=\text { angle between horizontal plane and } \\
& \text { upper deckboard at the ith support point due } \\
& \text { to distributed load between supports } \\
& (c l o c k w i s e \text { negative) (radians) and } \\
u \quad= & \text { distributed load (lb./in.). }
\end{aligned}
$$

Looking at Figure 3.7 it is apparent that ${ }^{\tau 1} 1_{1}$ and $\tau_{2}$ are equal in magnitude but opposite in direction for the assumed symetrical loads.

The end moments produced by the uniform load (Figure 3.7) on the overhang of the deck are calculated as:

$$
\begin{equation*}
M_{0}=(-u)\left(1^{\prime 2}\right) / 2 \tag{27}
\end{equation*}
$$

where:

$$
M_{0}=\text { moment at support point (in.-lb.). }
$$

Furthermore, Figure 3.8 shows the necessary equations used to calculate the angles, $\lambda 1_{1}$ and $\lambda I_{2}$ due to the applied end moments:

$$
\begin{align*}
& \lambda I_{1}=\frac{(u)\left(1^{\prime 2}\right)(1)}{4\left(E_{t}\right)\left(I_{t}\right)}  \tag{28}\\
& \lambda I_{2}=\frac{(-u)\left(1^{\prime 2}\right)(1)}{4\left(E_{t}\right)\left(I_{t}\right)} \tag{29}
\end{align*}
$$

$$
\lambda_{1}=\frac{\left(-M_{0}\right)(l)}{\left.(3) E_{t} \times I_{t}\right)} \wedge \lambda \lambda_{1} \lambda_{2}=\frac{\left(M_{0}\right)(l)}{(6)\left(E_{t}\right)\left(I_{t}\right)}
$$

$+$
$\lambda_{1}=\frac{\left(-M_{0}\right)(l)}{(6)\left(E_{t}\right)\left(I_{t}\right)}$

$=$
$\lambda_{1}=\frac{\left(-M_{0}\right)(\ell)}{\left.(2)\left(E_{t}\right) X I_{t}\right)}$


FIGURE 3.8 - An Illustration of how and are Calculated Utilizing the Principles of Superposition
where:

$$
\begin{aligned}
\lambda 1_{1} ; \lambda 1_{2}= & \text { angle between horizontal plane } \\
& \text { and top deckboard due to end moment } \\
& \text { (radians). }
\end{aligned}
$$

Since $\tau 1_{i}$ and $\lambda 1_{i}$ can be computed, then the total angular rotation due to loading (Figure 3.7) can be computed from:

$$
\begin{equation*}
\xi 1_{i}=\tau 1_{i}+\lambda 1_{i} \tag{30}
\end{equation*}
$$

In the Type I model $\phi 1_{1}$ and $\phi 1_{2}$ are assumed equal. With this in mind:

$$
\begin{gather*}
\beta 1_{1}=\phi 1_{1}-\xi 1_{1}=\phi 1_{1}-\frac{(u)(1)\left(\left(1^{2} / 6\right)-1^{\prime}\right)}{4\left(E_{t}\right)\left(I_{t}\right)}  \tag{31}\\
\beta 1_{2}=\phi 1_{2}-\xi 1_{2}=\phi 1_{2}+\frac{(u)(1)\left(\left(1^{2} / 6\right)-1^{\prime}\right)}{4(E)(I)} \tag{32}
\end{gather*}
$$

where:

$$
\begin{aligned}
\beta 1_{i}= & \text { total opening of the upper deckboard-i th } \\
& \text { stringer joint (Figure 11) for a Type II, } 2 . \\
& \text { stringer pallet (radians). }
\end{aligned}
$$

Equations (30) and (31) or (32) supply enough information to compute:

$$
\begin{equation*}
\beta 2_{i}=\xi 1_{i}+\beta 1_{i} \tag{33}
\end{equation*}
$$

where:

$$
\begin{aligned}
\beta 2_{i}= & \text { total opening of the lower deckboard- } \\
& i^{\text {th }} \text { stringer joint for a Type II, } 2 \text { stringer } \\
& \text { pallet. }
\end{aligned}
$$

Since all angles of the 2 stringer collapse specimen (Figure 3.7) can be computed, a K-factor can be calculated from:

$$
\begin{equation*}
K 1_{i}=\frac{\beta 1_{i}}{\phi 1_{i}} \quad ; \quad K 2_{i}=\frac{\beta 2_{i}}{\phi 2_{i}} \tag{34;35}
\end{equation*}
$$

where the $K$-factor is again based on the angular rotation of a Type I pallet. These $K$-factors are used in equation (24) to compute $h_{i}$.

## CHAPTER 4

## Experimental Verification

### 4.1 Introduction

Experimental verification of the ability of the model to predict $H_{\text {max }}$ was necessary to justify its use in design. Without strong support from experimental data the model will not be an accepted tool. This Chapter describes each step taken to verify the model.

## 4. $\underline{2}$ Development of $\underline{\text { a }}$ Lateral Load Test Machine

To physically measure the $H_{\max }$ of a full-size pallet a test machine was designed and constructed. The machine was capable of testing pallet sections with dimensions as small as $8^{\prime \prime} \mathrm{x} 30^{\prime \prime}$ and full-size pallets with dimensions as large as 72" x 72". Furthermore, the machine accomodates realistic unit loads and is capable of inducing a uniformly distributed horizontal load on the leading stringer of a test specimen. Eor simplification and consistency with the limitation of the theoretical model, the horizontal load was quasi-static in nature, rather than dynamic.

Figure 4.1 is a photograph of the test machine. The backbone of this machine (Figure 4.2) is made of three 4" wideflange I-beams each $12^{\prime}$ long. These lay on a concrete floor and are interconnected by one piece of $2.5^{\prime \prime}$ angle iron at each end. Holes are drilled every 4" throughout the length of the angle irons. The center I-beam always remains stationary unlike the two outer beams which are connected by bolts to the angle iron. This enables them to be moved to accomodate pallets whose stringers range from $8^{\prime \prime}$ to $72^{\prime \prime}$ in length.

Fastened perpendicular to the base I-beams is a $6^{\prime \prime}$ wideflange I-beam. This beam acts as a buttress for the load head. It is attached to the base I-beams by bolts which allow spacer blocks to be placed beneath the buttress Ibeam, thereby, allowing vertical adjustment.

A $10,000 \mathrm{lb}$. hydralic cylinder is attached by a swivel connection to the buttress I-beam. The controls and motor for the cylinder are stationed beside the test machine. A $4^{\prime \prime} \mathrm{x} 2.75^{\prime \prime}$, I-beam which is $72^{\prime \prime}$ long, is connected to the hydralic piston. Teflon coated slider blocks are mounted underneath the load head which rests on the two outboard base I-beams. Necessary vertical adjustments to the load


FIGURE 4.1 - Photograph of Test Machine


FiGURE 4.2-Plan and Profile Views of Test Machine
head are made by placing wood spacers beneath the slider blocks.

Finally, to prevent the test specimen from sliding when the horizontal load is applied, four restraining bars are attached to the machine. These bars are mounted perpendicular to the base I-beams and can be adjusted to any position parallel to the base. When testing skids, a restraining bar may be placed behind each stringer if desired. For testing double-faced pallets, a bar may be placed behind the last stringer to prevent specimen sliding.

A 10,000 lb. BLH type U3G2-S load cell was mounted in series between the hydralic cylinder and the load head. A Vishay amplifier sends an electronic signal from the load cell to a Hewlett Packard model 7044A X-Y recorder.

The Y-coordinate of the recorder plots horizontal translation of the upper deckboards of a test specimen. This is accomplished with two LVDT's which are mounted along any channel of the base I-beams. Two T-shaped brackets are attached to the upper deckboards of the test specimen and bear against the plunger of the LVDT's. For complete machine drawings, wiring, and operation see Appendix A. With the test machine complete, actual testing was ready to commense.

### 4.3 Model Verification: Type I

The objective of this section is to describe the experimental design and the analysis techniques used to determine the validity of the Type I model.

First, a computer program entitled "LCAN" (an acronym for Lateral Collapse ANalysis) was developed to caculate $H_{\max }$ using the Type I model. LCAN is written in the Fortran IV language, and is presented in Appendix B. The input parameters required to run this program are the geometric properties of the deckboards and stringers, the unit load applied to the structure, and the rotation modulus and maximum moment of each joint in the pallet. Once this data is entered and the program run, the output echoes the input data, the moments generated along each stringer, a predicted $H_{\text {max }}$, and a $H_{\text {max }} / V$ ratio.

To determine the accuracy of LCAN five full-size pallets, eight pallet sections, and eighteen joint rotation samples were built. All stringers and deckboards were oak (Quercus spp.) and had moisture contents above $30 \%$. The fasteners used were 2-1/4 inch long, helically threaded, low-carbon steel nails. They contained 4 flutes at 68 degrees with an
average thread crest diameter of 0.126 inches. The average MIBANT (25) angle of the nail was 46 degrees. All nails were meticulously placed in the patterns illustrated in Appendix Cl.

The pallets built were expected to behave as the Type I model. Refer to Appendix $C 2$ for construction specifications and for the unit load applied to test pallets. Testing was conducted on the lateral load machine with a cross-head rate of approximately 4 inches per minute. Figure 4.3 is a photograph of a test in progress. During each test a horizontal force (H) versus upper deckboard translation (X) curve was plotted (Figure 4.4). $H_{\max }$ was then determined from each curve for the test specimens (Table 4.1).

After testing the pallets, joint rotation samples were fabricated as described and to the dimensions specified in Table D1.1 of the Appendix. These samples were built to provide an estimate of $M_{\max }$ and $R$ was for use in LCAN. The joints were tested on a Tinius Olsen test machine with a cross-head rate of 0.015 inches per minute. During each test, a load-deflection curve was recorded and from it the $M_{\max }$ and rotation modulus were determined (Appendix DI.1). After each test, the MC and $G$ were determined for the


FIGURE 4.3 - Photograph of Collapse Test


FIGURE 4.4 - HORIZONTAL FORCE (LBS.) VS. HORIZONTAL
TRANSLATION (IN.) CURVE FROM COLLAPSE TEST

Table 4.1 Actual $H_{\text {max }}$ Versus Predicted $H_{\text {max }}$ for Type I Tests

deckboard and stringer components according to ASTM D-143 standards (1).

Once the testing was complete, each design was run through LCAN to predict $H_{\text {max }}$. Table 4.1 shows those values of $H_{\text {max }}$. It is apparent from the illustration that the model tends to under estimate $H_{\max }$ by an average of 579 lbs. or $19 \%$. This error could be from an under estimate of $M_{\text {max }}$ which can change because of the variability of wood's mechanical properties and/or the fastener characteristics.

A hypothesis was developed to explain this underprediction. This was that the slower rate of loading, 0.015 inches per minute in the joint rotation tests produced lower values for $M_{\max }$ and $R$ than were realistic for lateral collapse testing at 4 inches per minute. With these lower values the model would indeed under-predict $H_{\max }$.

A study was conducted to determine how the rate of loading influenced $M_{\max }$ and $R$. Thirty matched joint rotation samples were built according to the specifications in Appendix $C 3$ with nailing and stapling patterns as specified in Appendix Cl. Each type joint was tested at 4 inches per minute and 0.015 inches per minute with four repetitions each. A load-deflection curve was plotted
during each test and from these $M_{\max }$ and $R$ were determined. With this data a ratio of the $M_{\max }$ generated at 4 inches per minute to 0:015 inches per minute was computed (Table 4.2). The same procedure was performed for $R$ (Table 4.3). Tables 4.2 and 4.3 show the average $M_{\text {max }}$ and $R$ values of the joints tested in the study. Table D1.3 of the Appendix shows all of the test data. The results show a significant increase of $M_{\text {max }}$ and $R$ with the rate of loading.

With this new information on hand, all values from the initial joint rotation tests were increased by multiplying them by the appropriate ratio from Tables 4.2 and 4.3. Next, the Type I designs were re-analyzed using LCAN. The results show that the Type I model now over-predicts $H_{\text {max }}$ by an average of 188 lbs. or a $6 \%$ error (Table 4.4). This is obviously better than the original under-prediction.

It was concluded that the Type I model was an acceptable foundation for further investigation of lateral collapse; therefore, the next step in predicting LCP was to develop Kfactors that would modify the resisting moments in a Type II pallet.

Table 4.2 Average $M_{\max }$ Values for Modification Factor Analysis

| Fastener |  | $M_{\text {max }}$ |  | Ratio |
| :---: | :---: | :---: | :---: | :---: |
|  |  | Loadin | tes ${ }^{1}$ |  |
| Type | \# | 0.015 | 4.0 | 0.015/4 |
| nail | 4 | 908 | 1100 | 1.211 |
| nail | 3 | 750 | 1038 | 1.384 |
| staple | 3 | 582 | 670 | 1.151 |
| staple | 1 | 183 | 232 | 1.270 |
|  |  |  |  |  |

${ }^{1}$ Rates are inches/minute

Table 4.3 Average $R$ Values for Modification Eactor Analysis

| Fastener |  | Rotati | dulu | Ratio |
| :---: | :---: | :---: | :---: | :---: |
| Type | \# | 0.015 | 4.0 | 0.015/4 |
| nail | 4 | 2115 | 2818 | 1.332 |
| nail | 3 | 1956 | 2261 | 1.156 |
| staple | 3 | 1396 | 2375 | 1.703 |
| staple | 1 | 537 | 804 | 1.497 |
|  |  |  |  |  |

${ }^{1}$ Rates are inches/minute

## Table 4.4 Actual $H_{\text {max }}$ Versus Predicted $H_{\text {max }}$ after Re-analysis of Type I Tests

| Specimen No. | $\begin{gathered} \text { Actual } \\ H_{\max } \\ (1 b .) \end{gathered}$ | $\begin{gathered} \text { Predicted } \\ \mathrm{H}_{\max } \\ (1 \mathrm{lb} .) \end{gathered}$ |
| :---: | :---: | :---: |
| 1 | 1188 | 1482 |
| 2 | 1200 | 1482 |
| 3 | 1525 | 1579 |
| 4 | 1563 | 1579 |
| 5 | 738 | 2026 |
| 6 | 2575 | 2778 |
| 7 | 2375 | 2825 |
| 8 | 2825 | 3315 |
| 9 | 4200 | 3424 |
| 10 | 4200 | 3424 |
| 11 | 5300 | 4942 |
| 12 | 4725 | 4942 |
| 13 | 6880 | 7931 |
|  |  |  |
| Average | 3022 | 3210 |

### 4.4 Model Verification: Type II

This section presents the methods and materials used to develop and verify the moment modification factor for Type II pallets. Because of the complexity of the combined bending-axial force actions in Type II pallets, some simplifications were necessary. Consider the stringer pallet shown in Figure 3.6. If there is significant flexure in the top deckboards then many $\phi_{i j}$ values will be dissimilar. The magnitude of an individual $\phi_{i j}$ will be a function of the actions of the vertical force causing deck flexure as well as that of the horizontal force causing collapse. Compared to a Type I pallet some of the Type II joints will have reached $M_{\max }$ while others will still undergo elastic rotation. Hence the difference in rotation compared to the Type I pallet will lead to an erroneous prediction of $H_{\text {max }}$ using the Type I analog model procedure.

To develop correction factors for three and four stringer Type II pallets the structural analysis program SPACEPAL (17) was used. This program calculates the moments at each joint for a given horizontal load. Initially, one SPACEPAL model was developed for three stringer pallets and one for
four stringer pallets. These analog models are shown in Appendix B2. These models are inherently unstable and some initial horizontal force, $H_{e q}$, is needed to insure initial stability. Additional horizontal force will cause clockwise rotation simulating lateral collapse.

A wide range of pallet styles, from expendables to warehouse-type designs, were modeled with SPACEPAL to determine the influence of various parameters on joint moments. The three study variables were a) $E_{t} I_{t} / l^{3}$ of the top deckboards, b) stringer aspect ratio $\left(d_{i} / w_{i}\right)$, and c) the joint characteristics - $M_{\max }$ and $R$. Appendix Tables B3.1 and B3.2 describe all 27 designs of the three and 27 designs of the four stringer, double-faced pallets, respectively. Additionally, 18 single-faced three and four stringer pallet designs specified in Tables B3.3 and B3.4 of the Appendix were also analyzed for a total of 72 computer models. Each model was submitted to SPACEPAL and analyzed with 500, 2250, and 5000 lb . unit vertical loads. All 72 designs were initially run through LCAN to determine the Type I $H_{\text {max }}$ and $M_{\text {max }}$. The total horizontal load ( $H_{\text {tot }}$ ) applied to each model was the Type I $H_{\max }$ from LCAN plus $\mathrm{H}_{\mathrm{eq}}$.

The resulting theoretical moments developed at each joint were recorded and individual $K_{i j}$ were computed using equations (22) and (23). Multiple regression equations between $K_{i j}$ and unit load, deck MOE, deck moment of inertia, stringer width and height, $M 1_{i}$ and $M 2_{i}$ were derived for the three stringer and four stringer pallets. The result was one different regression equation for each joint in the structure (Appendix D2). For example, twelve equations were developed for a four stringer double-faced pallet representing one for each joint. $R^{2}$ values for individual joint regressions were consistantly high.

Use of the twelve regression equations provides the best possible estimate of the needed modifications for Type II behavior. However, this approach is far too cumbersome for general design use. A second set of regression equations was developed by combining all K-factors from pallets with the same number of stringers. Therefore, one regression equation was used for three stringer and one equation for four stringer pallets. The three and four stringer regressions are presented in equations (36) and (37), respectively:

$$
\begin{gather*}
K_{3}=0.8956+0.0003(V)+0.0013\left(E_{t}\right)\left(I_{t}\right) / e^{3}  \tag{36}\\
-1.6004(\mathrm{Ar})+0.0001\left(M_{\max }\right)
\end{gather*}
$$

$$
\begin{gather*}
K_{4}=0.1306-0.00001(V)+0.0494\left(E_{t}\right)\left(I_{t}\right) / e^{3}  \tag{37}\\
-0.0569(A r)-0.00002\left(M_{\max }\right)
\end{gather*}
$$

where:

$$
\begin{aligned}
K_{k}= & K-f a c t o r \text { for three and four stringer pallets } \\
& \text { and } \\
A r= & w_{i} / d_{i} \text { of stringers (in./in.). }
\end{aligned}
$$

The R-square value for equations (36) and (37) was 0.358 and 0.579, respectively.

To evaluate this simplified approach, equations (36) and (37) were implemented into LCAN and the 72 pallet designs were re-analyzed. Although the regression equations developed for each individual joint are likely to be more accurate than the second set, the number and complexity of the equations must be reduced without a significant loss of accuracy. The output of LCAN produced two $H_{\max } / V$ ratios $\mathrm{H}_{\max } / \mathrm{V}$ and $\mathrm{H}_{\max } / \mathrm{V}$ - for each design. $\mathrm{Hl}_{\max } / \mathrm{V}$ was computed using a unique $K$-factor equation for each joint and $\mathrm{H} 2_{\max } / \mathrm{V}$ was computed with only one $K$-factor equation. Next, the two sets of ratios were ranked from lowest to highest. As stated previously, the $\mathrm{Hl}_{\max } / \mathrm{V}$ order of rank was considered to be the most accurate. The $\mathrm{H} 2 \max / \mathrm{V}$ rank was then compared to the $\mathrm{Hl}_{\text {max }} / \mathrm{V}$ rank.

The purpose of the comparison was to note where each design fell in the $\mathrm{Hl}_{\max } / \mathrm{V}$ rank versus where it fell in the $\mathrm{H} 2_{\text {max }} / \mathrm{V}$ rank. For example, if in the $\mathrm{H} 1_{\text {max }} / \mathrm{V}$ rank a particular design was ranked $29^{\text {th }}$ and the same design was ranked $34^{\text {th }}$ in the $\mathrm{H} 2_{\max } / \mathrm{V}$ rank, the difference would be -5 . The differences were determined for each of the 72 pallet designs. Then, the mean and standard deviation was determined for the differences. If a low standard deviation was found then one regression equation, (36) or (37), would be used in the Type II model. This is because the one equation would do as good a job modifying the moments as would the individual equations for each joint.

The results of the three stringer case showed a mean difference of zero with a standard deviation of 5.3. Figure 4.5 illustrates that the change in rank was random and showed no bias towards any one group of $\mathrm{H}_{\text {max }} / \mathrm{V}$ ratios. Therefore, the assessment of a pallet's lateral collapse potential based on its $H_{\max } / V$ ratio would not be significantly altered using equation (36).

In the four stringer case the mean difference was again zero with a standard deviation of 6.1. Figure 4.6 shows random and unbiased changes in ranks. Based on these


FIGURE 4.5 - THE CHANGE IN RANK OF H2MAX/V VERSUS THE HIMAX/V RANK FOR 3 STRINGE? PALLE:S


FIGURE 4.6 - THE CHANGE IN RANK OF H2MAX/V VERSUS THE H1MAX/VRANK FOR 4 STRINGER PALLETS
analyses, it was concluded that equations (36) and (37) would provide acceptable K -factor predictions.

## 4. 5 Experimental Verification of LCAN

A series of 18 different pallet designs were selected for an experimental verification of the lateral collapse analysis procedure. These designs were selected to represent a range of expected $H_{\text {max }} / V$ ratios and different geometries. Six geometries of each two, three and four stringer designs were chosen.

The pallet shook used to build the test specimens were of aspen (Populus), oak (Quercus), and yellow poplar (Liriodendron tulipifer). Each had a moisture content above $8 \%$. The oak and poplar were used for stringer material and the oak and aspen for deckboards. The pieces were manufactured in final dimension and stored.

The fasteners used were the same helically threaded nail previously described in Chapter 4 plus a 15 gauge, 2-1/4 $x$ $0.074 \times 0.067$ inches, uncoated staple. The MIBANT angle of the staple was 132 degrees as predicted by Padla (20).

To estimate the value of $M_{\max }$ and $R$ of stapled joints, six rotation samples with three replications, were built as specified in Appendix C2 and D1.2. Testing was conducted on the Tinius Olsen test machine with a cross-head rate of 0.015 inches per minute. A load-deflection curve was plotted during each test and from these, $M_{\max }$ and $R$ were determined (Appendix D1.2). After testing, MC and G of the deckboard and stringer were determined according to ASTM D-143 standards. No nail joint tests were conducted since the pallet shook (oak) used to build these specimens came from the same stack of shook that was used to build the Type I test specimens. It was assumed that the joint characteristics were similar.

The dimensions of the deckboard material used were measured to the nearest 0.001 inch. Each board received an identification number, and its $E$ (Appendix C4) was determined by the dead-weight deflection method (21).

Knowing the deckboard dimensions, E-values, and predicted joint characteristics, LCAN was used to analyze the eighteen test geometries. These results showed that the actual test pallets had theoretical $H_{\text {max }} / V$ ratio's ranging from 0.3 to 2.5.

The eighteen pallets were built according to the specifications in Appendix $C 5$ with nailing and stapling patterns as specfied in Appendix C1. These pallets were tested on the lateral test machine with an approximate cross-head rate of 4 inches per minute. During each test a $H$ versus $X$ curve was generated. From these curves, $H_{\text {max }}$ was determined (Table 4.5).

After modifing $R$ and $M_{\max }$ for rate of loading, all of the Type II pallets were analyzed with LCAN. The results presented in Table 4.5 shows that the average difference in $H_{\text {max }}$ was a 269 lb. over-estimate or a $14.5 \%$ error. There was no evidence from the analysis that the model was less accurate at any one particular $H_{\max } / V$ ratio compared to another. Material variability, accuracy in load placement during test and the use of simplified equations (36) and (37) to generate the $K$-factors all contributed to the error. However, for the purpose of this study this error is quite resonable and it is concluded that the model provides an acceptable means of assessing.the lateral collapse potential of a pallet.

To determine the influence of the $K$-factors on the computation of $H_{m a x}$ the pallets in Table 4.5 were re-

Table 4.5 Actual $H_{\text {max }}$ Versus Predicted $H_{\text {max }}$ for Type II Tests

| Specimen No. | $\begin{gathered} \text { Actual } \\ \mathrm{H}_{\max } \\ (\mathrm{lb} .) \end{gathered}$ | $\begin{gathered} \text { Predicted } \\ \mathrm{H}_{\max } \\ \text { (lb.) } \end{gathered}$ |
| :---: | :---: | :---: |
| 1 | 588 | 783 |
| 2 | 925 | 1060 |
| 3 | 1100 | 1210 |
| 4 | 1225 | 1271 |
| 5 | 1400 | 1580 |
| 6 | 1643 | 1739 |
| 7 | 1188 | 1450 |
| 8 | 1818 | 2072 |
| 9 | 1862 | 1962 |
| 10 | 1762 | 2146 |
| 11 | 2087 | 2200 |
| 12 | 2250 | 2195 |
| 13 | 2275 | 2439 |
| 14 | 2125 | 2693 |
| 15 | 2450 | 2733 |
| 16 | 2375 | 2999 |
| 17 | 2725 | 3372 |
| 18 | 3500 | 4238 |
| Average | 1850 | 2119 |

analyzed without using the K-factors. The results show an average 678 lb . over-estimate of the actual $H_{\text {max }}$ or a $37 \%$ error. Erom this analysis it was concluded that the $K$ factors significantly improve the prediction of $H_{\max }$ and, therefore, deserve a place in the model.

## CHAPTER 5

Design Procedures and Calibration

### 5.1 Introduction

The global objective of this investigation was to develop a design methodology that would evaluate the LCP of pallets. At this point in the investigation the model would predict $\mathrm{H}_{\text {max }} / \mathrm{V}$ ratio. For design purposes a "yardstick" must be developed to determine acceptable and unacceptable ranges of $\mathrm{H}_{\text {max }} / \mathrm{V}$.

## 5. 2 Field Survey and LCP Categories

For this purpose, it was necessary to locate pallets that had experienced lateral collapse. The designs collected form the basis of a definition of the transition points between LCP categories of acceptable and unacceptable. Forty manufacturers across the United States were surveyed. While fourteen of those surveyed had some type of experience with collapsing pallets, only two well documented designs
were found. Their design specifications and unit loads at the time of collapse are specified in Appendix C6. Each of the designs had three stringers with very low aspect ratios and were fastened with staples. Their $H_{\text {max }} / V$ ratios were determined to be 0.47 and 0.50 by LCAN. $A H_{\max } / V$ ratio of 0.50 indicates that these designs could only withstand a horizontal load no greater than one half the unit load. Adding a safety factor of 0.10 to the $H_{\max } / V$ ratio of 0.50 equals 0.60 which was defined to be the point between high and medium LCP risk categories.

Since has been impossible to obtain field data on those pallets that are in the medium and low risk categories, 1.0 was arbitrarily selected to be the transition point between these categories. A pallet with this $H_{\text {max }} / V$ ratio could only withstand a maximum horizontal load equal to its unit load. In all probability, pallets in the field are going to experience a horizontal load of this magnitude. Due to this likelihood, it was felt that those pallets that have a 0.60 $<H_{\max } / V<1.00$ should be classified in the medium risk collapse category. The two LCP transition points were believed to be the best choices based on the available field data and collapse theory.

## 5. 3 Implementation into PDS- the Pallet Design System

After verification of the design method, a condensed version of LCAN was incorporated as a subroutine in the NWPCA's PDS computer program.

Because of the limitations set on the data input, the PDS program must calculate $M_{\max }$ using equation (38):

$$
\begin{equation*}
M_{\max }=\left(w_{i} / 2\right)(\text { Separation factor }) \tag{38}
\end{equation*}
$$

where:

$$
\begin{aligned}
M_{\text {max }}= & \text { maximum moment a joint can sustain } \\
& \text { (in.-lb.) and } \\
\text { Separation factor }= & \text { joint withdrawal resistance } \\
& \text { (lbs.) which is the lesser } \\
& \text { value of equations (2), (3) or } \\
& (4) .
\end{aligned}
$$

To evaluate the accuracy of equation (38) a predicted $M_{\text {max }}$ was calculated for each joint rotation sample tested in this experiment (Appendix D1). A comparison between the $M_{\text {max }}$ calculated with equation (38) versus the actual $M_{\text {max }}$ is shown in Appendix D1. The tables show an under-estimate of $M_{\text {max }}$ averaging 63 in.-lbs. Note that in Table DI. 3 some of the $M_{\max }$ predicted values are missing. This is because these are the joints that were tested at the faster rate of
loading which equation (38) will not predict. With the limited data from this investigation this method of predicting $M_{\max }$ was considered the best available for the PDS program.

### 5.4 Documented Lateral Collapse Failures

Since PDS has been in use, three pallet designs that have failed in lateral collapse have been documented. Their specifications are in Appendix Table C6 as pallets \#3, \#4 and \#5.

Designs \#3 and \#4 are three stringer, single-faced pallets fastened with very low quality, helically threaded nails. During their service lives, each design was expected to sustain a maximum unit load of 2500 lbs . When the designs are run through PDS their $H_{\max } / V$ ratios equal 0.90 and 0.87 , respectively. These ratios fall within the medium collapse potential category which should indicate to a pallet designer that there is a chance of lateral collapse occuring.

Pallet \#5 is a shipping pallet whose $H_{\max } / V=0.62$ indicates a high to medium risk design. Utilizing the lateral collapse model a pallet designer might expect this design to collapse. To decrease the probability of failure this pallet's geometry, material properties, and/or its fastener characteristics should be changed.

## 5. $\underline{5}$ Variable Sensitivity

After using PDS, a pallet designer should begin to sense that there are four major variables that influence a pallet's LCP. Each individual pallet designer must consider which of the four variables are the most economically feasible to change in his situation.

Figure 5.1 illustrates the effects of aspect ratio on $H_{\text {max }} / V$. As this ratio increases, the pallet becomes more resistant to lateral collapse. One explanation of this change is that as the stringer height is reduced, the leverarm distance $\left(Y_{i}\right)$ of $h_{i}$ is decreased, and, therefore, $H_{\max }$ increases. Similarly, as the lever-arm distance ( $Z_{i}$ ) of $V_{i}$ is increased by increasing the stringer width, the resisting moment is increased. Thus, $H_{\max }$ increases as well. Also,


FIGURE 5.1 - THE EFFECT STRINGER ASPECT RATIC has on the hmax /V ratio
as the number of stringers increases, the LCP decreases. Using this information, a designer can increase the $H_{\text {max }} / V$ ratio of a pallet by increasing its stringer aspect ratio. This finding was expected according to Gregory's (7) stability theory.

Eigure 5.2 illustrates the effect of unit load on a pallet's LCP. As the load is increased, the potential for lateral collapse is increased. More specifically, the upper deckboards will experience greater amounts of initial deflection because the larger loads will tend to open the deckboard-stringer joints. As a result, the total amount of resisting moment from the joints decreases which, in turn reduces $H_{\text {max }}$. Since it is quite possible for a pallet to be subjected to a wide range of unit loads, it is important during the design process to have relative feel for the largest unit load the pallet will support.

Another variable that influences the LCP of a pallet is its $E_{t} I_{t}$ of the upper deckboards (Figure 5.3). As this variable is increased the $H_{\max } / V$ ratio will increase up to a point where the $K$-factor equation predicts no deckboard bending. Beyond this point, no increase in $H_{\max } / V$ can be accomplished. Decrease in pallet $L C P$ might be more readily


FIGURE 5.2 - THE EFFECT UNIT LOAC HAS


FIGURE 5.3 - the effect of flexural qigidity ON HMAX/V
and economically accomplished by changing one of the other three variables discussed in this Chapter.

The type and number of nails used in the pallet will have an effect on the $M_{\max }$ and rotation modulus. Figure 5.4 shows that as $M_{\max }$ increases the $H_{\max } / V$ ratio does the same because of the greater resistance to overturning. Therefore, if it is feasible to add another nail per joint or to increase nail quality, a significant reduction in LCP will result. This is likely to be the most economically attractive means of improving resistance to lateral collapse.


FIGURE 5.4 - THE EFFECT MAXIMUM MOMENT
PER JCINT HAS ON HMAX/V

## CHAPTER 6

## Conclusions

A model of static lateral collapse of wood pallets was proven to perform satisfactorily. A relative measure of lateral collapse potential was determined by the $H_{\text {max }} / V$ ratio. Based on limited field data, if the $H_{\max } / V$ ratio is in the range zero to 0.60 , the pallet design is in a high risk category, between 0.60 and 1.00 it is in a medium risk category, and from 1.00 to infinity it is in low risk category.

Those factors that influence the LCP are:

1) Stringer Aspect Ratio $\left(w_{i} / d_{i}\right)$ - As this ratio is increased the collapse risk is decreased.
2) Upperdeckboard $\left(E_{t}\right)\left(I_{t}\right) / l^{3}$ - An increase of this property will increase the lateral collapse resistance up to a point where no deckboard bending occurs and beyond this point, LCP remains constant.
3) Joint Characteristics - The LCP of a pallet will decrease as the maximum moment and rotation modulus of the joints in the pallet are increased.
4) Unit Load - As the unit load on the pallet is increased, the risk for lateral collapse increases.

## LITERATURE CITED

1. American Society for Testing Materials. 1983. Standard Methods of Testing Small Clear Specimens of Timber. ASTM Designation D143-52. Annual Book of ASTM Standards, Vol. 4.09, pp. 61-62.
2. Antonides, C.E., M.D. Vanderbilt, and J.R. Goodman. 1980. Interlayer Gap Effect on Nailed Joint Stiffness. Wood Science 13(1): 4-46.
3. Blockley, D.I. 1980. The Nature of Structural Design and Safety. John Wiley and Sons, New York.
4. Bodig, J. and B.A. Jayne. 1982. Mechanics of Wood and Composites. Van Nostrand Reinhold Co. Inc., New York. p 252.
5. Dunmire, D.E. 1966. Effects of Initial Moisture Content on Performance of Hardwood Pallets. USDA Forest Service Research Paper NC 4, June.
6. Goehring, C.B. and W.B. Wallin. A Survey of Loads, Loading Conditions for Wooden Pallets. Unpublished. Northeastern For. Expt. Station. Princeton, W.V.
7. Gregory, M.S. 1967. Elastic Instability. E. and F.N. Spon Limited, London. p 1-33.
8. Hoyle, R.J.Jr. 1978. Wood Technology in the Design of Structures. Mountain Press Publishing Co., Montana. p 31 .
9. Johnston, B.G. 1976. Guide to Stability Design Criteria for Metal Structures. John Wiley and Sons, New York. p 18-80.
10. Kyokong, B. 1979. The Development of a Model of the Mechanical Behavior of Pallets. Thesis. Va. Tech, Blacksburg, Va.
11. Langhaar, H.L. and A.P. Boresi. 1959. Engineering Mechanics. McGraw-Hill Book Co., Inc. Pa.
12. Loferski, J.R. Literature Review - Design Procedures for Wooden Pallets. Unpublished. Va. Tech, Blacksburg, Va.
13. Mack, J.J. 1966. The Strength and Stiffness of Nailed Joints Under Short Duration Loading. Tech. Paper No. 40. Div. of For. Prod., C.S.I.R.O., Melborne, Australia.
14. Mack, J.J. 1975. Contribution of Behavior of Deckboard-Stringer Joints to Pallet Performance. Wd. Res. and Wd. Construction Lab. Bull. No. 136, Va. Tech, Blacksburg, Va.
15. McCurdy, D.R. and D.W. Wildermuth. 1981. The Pallet Industry in the United States 1980. Dept. of Forestry. So. Ill. Univ. 1981.
16. Meriam, J.L. 1978. Engineering Mechanics: Statics and Dynamics. John Wiley and Sons, New York. p 190.
17. Mulheren, K. 1982. SPACEPAL. Computer program. Va. Tech, Blacksburg, Va.
18. National Eorest Products Association. 1982. National Design Specifications for Wood Construction. N.E.P.A., Washington, D.C.
19. N.W.P.C.A. 1962. Specifications and Grades for Warehouse, Permanent or Returnable Pallets of West Coast Woods. N.W.P.C.A., Washington, D.C.
20. Padla, D.P. 1983. Relationships Between MIBANT Bend Angles and Selected Material Properties of Pallet Fasteners. Thesis. Va. Tech, Blacksburg, Va.
21. Percival, P.H. 1981. Portable E-tester for Selecting Structural Component Lumber. Forest Products Journal 3(2): 39-42.
22. Protective Packaging Group. 1976. Reusable Wood Pallets: Selection and Proper Design. E. For. Prod. Lab. Ottawa, Canada. Eor. Tech. Report 11.
23. Pugsley, A.G. 1966. The Safety of Structures. Edward Arnold (Publishers) LTD., London. p 1-53.
24. Randall, F.A.Jr. 1973. Historical Notes on Structural Safety. A.C.I. Journal Oct. p 669.
25. Stern, G.E. 1970. The MIBANT Quality Control Tool for Nails. Wd. Res. and Wd. Construction Lab. Bull. No. 100, Va. Tech, Blacksburg, Va.
26. Wallin, W.B. and E.G. Stern. 1974. Design of Pallet Joints from Different Species. N.E. Eor. Expt. Station.
27. Wallin, W.B. and E.G. Stern. 1974. Tentative Performance Standards for Warehouse and Exchange Pallets. For. Prod. Mkting. Lab., Princeton, W.V.
28. Wallin, W.B., E.G. Stern, and J.A. Johnson. 1976. Determination of Flexural Behavior of Stringer-type Pallets and Skids. Wd. Res. and Wd. Construction Lab. Bull. No. 146, Va. Tech, Blacksburg, Va.
29. Wallin, W.B., K.R. Whitenack. 1982. Durability Analysis for Wooden Pallets and Related Structures. N.E. Forest Experimentation Station. Princeton, WV. p 23-26.
30. West, H.H. 1980. Analysis of Structures. John Wiley and Sons, New York. p 27-29.
31. White, M.S. 1983. Personal Communications. Va. Tech, Blacksburg, Va.
32. U.S.D.A. For. Serv. 1974. Wood Handbook, For. Prod. Lab. Agri. Handbook. No. 72.

## APPENDIX A

Al - Machine Drawings
A2 - Machine Wiring
A3 - Machine Operation
A3.1 - Pre Test Calibration Procedures
A3. 2 - Typical Test Procedures

Al - Machine Drawings



Scale 1" = 1'
FIGURE A1.1 - End Profile Views of Test Machine


FIGURE A1.2 - Plan and Profile Views of Buttress-Load Head Connection


## A2 - Machine Wiring



FIGURE A2.1 - Electrical Wiring Diagram of Test Machine

A3 - Machine Operation

A3.1 - Pre Test Calibration Procedures

1) Calibrate 10;000 lb BLH load cell according to procedures outlined in its specifications manual. Install load cell on machine.
2) Turn on VISHAY amplifier, Hewlet-Packard X-Y recorder and the two LVDT power supplies for a 10 minute warm-up.
3) Check LVDT power supplies for a 23.81 volt output.
4) Check bridge voltage of channel 4 which sould be 12.00 volts. Adjustment is made with "BRIDGE EXCIT."
5) With "EXCIT" switch off, balance lights on VISHAY with the "AMP BALANCE."
6) Turn "EXCIT" switch on. Balance VISHAY lights with "BALANCE" knob.

A3. 2 Typical Test Procedures

1) Place LVDT brackets in desired location along channel of base I-beams. Tighten 4 screws in each bracket.
2) Insert LVDTs into brackets, and tighten thumb screws.
3) Place test specimen on machine in desired location (about 1.5" away from retracted load head).
4) Adjust load head height with spacer blocks so that contact is made on upper deckboard.
5) If desired, slide restraining bars to appropriate positions. Tighten all bolts.
6) Loosely attach T-brackets on the upper deckboards so that the stem of the $T$ is directly forward of the LVDT plunger. Slide $T$-bracket towards the load head causing the plunger to retract $2 / 3$ original length. Thighten brackets.
7) Calibrate $X-Y$ recorder by placing $0.015^{\prime \prime}$ gauge blocks between LVDT plunger and T-bracket.
8) Repeat step 7 for other LVDT.
9) Check VISHAY lights for their balance. Make necessary adjustments.
10) Place unit load on specimen.
11) Turn on hydralic motor.
12) Switch the "DIRECTION" switch up on the hydralic control box.
13) Bring load head forward by turning motor "SPEED" switch. Stop prior to contacting specimen.
14) Check the unit load's stability!
15) Adjust $X-Y$ recorder pen to desired location.
16) Control load during test with hydralic "SPEED" switch.
17) Once the $X-Y$ recorder indicates maximum horizontal load, turn the "SPEED" switch to zero.
18) Move "DIRECTION" switch to the down position until load head is fully retracted.
19) Turn off hydralic motor.

## APPENIX B

```
B1 - Listing of LCAN Program
B2 - Analog Models
B3 - Pallet Designs for Computer
    B3.1 - Three Stringer, Double-Faced Pallets
        Designed for K-Factor Development
    B3.2 - Four Stringer, Double-Faced Pallets
        Designed for K-Factor Development
    B3.3 - Three Stringer, Single-Faced Pallets
        Designed for K-Factor Development
    B3.4 - Four Stringer, Single-Faced Pallets
        Designed for K-Factor Development
```



THIS PROGRAM COMPUTES THE LATERAL FORCE-DISPLACEMENT RELATIONSHIP Of A PALIET, SINGLE- OR DOUBLE-FACED, SUBJECT TO A UNIT LOAD AND A IIORIZONTAL FORCE (H).
D.L.ARRITT SEPT. 22.1983

REFERENCE: T.E.MCIAIN. 1983. 'LATCOL'.
LAST UPDAIE WAS APR. 18, 1984

DIMENSION $W(4), D(4), V(50), O F(4), J P(4), A S(4), Z(4), Y(4)$,
$\operatorname{HHV}(4), \operatorname{HJ}(4), \mathrm{B}(4), \mathrm{BS}(11), \operatorname{PHI}(4), \operatorname{INFO}(80), \operatorname{HVMAX}(4), \operatorname{HJMAX}(4)$,
\#DP(4), DPMAX(4), HLN(1) , HS (150), XS (150), NJT(4), PHICR(4)

*BCRVI (4), BCRVB (4), RMXAT (4), RHXBT (4), RMXAB (4), RMXBB (4)
*RMOM1 (1) , $\operatorname{RMOM2}(4), \operatorname{RMXT}(4), \operatorname{RHMB}(4), \operatorname{RMAX1}(4), \operatorname{RMAX2(4),Z1(4),~}$
*Z2(4),Z3(4),Z4(4),E(4), Bi(4),D1(4),NOBDS(4),H(16)

READ IN PALLET VARIABLES FRON DATA FILE
$\operatorname{READ}(5,5)(I N F O(1), I=1,80)$
IOKMAT (40AZ)
READ (5, 10) LIVEL,AY, IA
FORMAI (T14, 11, T25, A3, T28, 12)
REAI) (5, 15) NJP,NINC, XINC, VOF, NOSTR, JOP
FORMAT $(/ /, 215,2$ F10.3,215,//)
(O) $201=1, N J P$

IREAD (5,25) XJTOP(I), XJBOT(I)
rORMAT (2F10.1)
COHI INUE

NJP= NO. OF JOINIS WITH DIFFERENT PROPERTIES
NINC= NO. OF INCREMENTS OF HORIZONTAL DISPLACEMENT
XINC= SIZE OF INCRFMENTS
VOF = VERTICAL OFFSET (I.E. SIZE OF LATERAL RESTRAINT PIATE)

```
    ZERO FOR DOUBLE.-FACED PALLETS
    NOSTIR= NO. OF SIRINGERS
    JOP= TYPE OF PALLET 1) SINGLE-FACED=1
                                    DOUBLE-FACED=2
XJIOP18:2= # OF JOINTS ALONG THE TOP OF EA. STR.(I) WITH JOINT
XIBOT1R.2= PROP. (I) OIS ALONG THE BOTTOM OF EACH STR. (I) WITH
XJBOT1R2= # OF JOINIS ALONG THE BOTTOM OF EACH STR.(I) WITH
    JOINT PROP.(I)
    IF(LEVEL.EQ.3)GO TO 70
    WRITE (6,30)
    FORMAT (' 1',' INPUT DATA',/)
    WRITE (6,35) (INFO(I),I=1,80)
    TORINAT (40A2/40A2)
    WRITE (6.10)
FORMAT(//, 18,'NJTOP(I)',T42,'NJBOT(I)')
DO l/5 I=1,NJP
    WKITE (6,50)XJTOP(1),XJBOT(1)
    FORMAT(1X, T3,F10.1, T37, F10.1)
CONTINUE
WRITE (6,55)
FORMAT('//,T8,'NJP',T19,'NINC',T31,'XINC',T43,'VOF',T54,'NOSTR'.
#'GL,'JOP';
    FURMAT (1X,15,15,T17,15,T26, F10.3,T37, F10.3,T52, I5,T61, I5)
    READ IN PALLET VARIABLES FROM DATA FILE
    W(I),D(I)= WIDTH AND HEIGHT OF EACH STRINGER
    V(I)= VERTICAL FORCE ONTOP OF EACH STRINGER
    JP(I)= JOINT PROPERTY NO. OF EACH STRINGER
                0 INDICATES 2 DIFFERENT JOINTS ALONG STR.(1)
            1 "llllll
OF(I)= FINAL OFFSET OF EACH STRINGER= DISTANCE FROM EDGE
            TIIAT VERTICAL FORCE VECTOR ACTS AFTER SOME DEFORMATION
            IIIAT VERIICAL FORCE VECTOR ACTS AFTER SOME DEFORMATION
            CHANGES WITH INCREASING }X\mathrm{ .
```

```
WRII: . !
```

WRII: . !
IORI:A:...: IO, 'WIDTH', T24, 'DEPTH', T34,'J.P.')
IORI:A:...: IO, 'WIDTH', T24, 'DEPTH', T34,'J.P.')
CONI INUE.
CONI INUE.
READ (5,75)
READ (5,75)
I ORMAT (//)
I ORMAT (//)
D) 80 $1=1$, NOSTR

```
D) 80 \(1=1\), NOSTR
```

REAI) $(5,85) W(1), D(1), J P(I)$
FORMAI (2F10.3.15)
IF (LEVEL.EQ. 3 )GO TO 80
WRITE (6,90) W(1),D(1),JP(1)
1OMRAI (ix,17,f7.2.121,F7.2.T30,15)
CONIIRUE.

AS IHF DATA [NTERS THIS DO-IOOP, ONE OF THE NJT'S WILL BE ASSICNIO FOR EACH NJP. THE ROTATION MOHENTS OF THE JOINTS ARI COHPUIID BY FUULTIPLING XJTOP(I) AND XJBOT(I) WITH THE rOLISOWING VALUES:

NJJ=0 ONLY MAX. MOHENT KNOWN
RMXBI \& RMXBB= MAX. MOM. JOINT CAN SUSTAIN
NJT=1 BII.INEAR MOH. - THETA CURVE
BIOF \&C BBOT= INITIAL SIOPE OF MOM. - THETA CURVE
RHXBT \& R RMXBB = MAX. MOM. JOINT CAN SUSTAIN
NJT $=2$ TRILINEAR MOH. - THETA CURVE
ACRVI \& ACRVB = INITIAL SLOPE OF MOM. - THETA CURVE
BCRVT \& BCRVB= SLOPE OF SECOND LINE ON MOM. - THETA CUṘVE
RMXAT \& $R M X A B=$ MAX. MOM. OF ACRV.
RMXBT \& FRMXBB= MAX. MOM. OF BCRV.
NJT $=3$ POWER FUNCTION MOM. -THETA CURVE
MOH. $=($ ACRVT + ACRVB)*(THETA(RAD.) )**(BCRVT OR BCRVB)
RMXAT \& RMXAB= MAX. MOM. JOINT CAN SUSTAIN

READ (5,75)
DO $155 \quad i=1$, N.JP
IF(LEVEI.EQ. 3)GO TO 105
WRIIE 6,100$)$
FORMAT (//, T2, 'NJT', T12, 'Z1', T22, 'Z2', T32, 'Z3', T42,'Z4')
CONIINUE.
READ (5,110) NJT(I),Z1(I),Z2(1),Z3(I), Z4(1)
FORHAT (15, IF10.3)
IF(LEVEL..EQ.3)GO TO 115
WRITE (6,120) N.JT(I),Z1(I), Z2(I),Z3(I), Z4(1)
FORMAT (1X, 11, T7, F10.3, T17,F10.3, T27, F10.3, T37, F10.3)
conrifue
IF (NJI(I).EQ.D) GO TO 125
IF (NJT(I).EQ.2) (CO TO 130
IF N.II(I).EQ.3) GO TO 135
$1310 P(1)=x J 10 P(1) * Z 1(1)$
BBOI( 1 ) =XJBOT(1)*Z1(1)
KMXBI (1) $=\times$ XITOP $(1) * 22(1$
RMXBB(I)=XJBOI(1)*Z2(1)

```
IF(LEVEL.EQ.3)CO TO 140
    WRITE (6,145)
    IORHAI(1X,T10,'BTOP',T26,'BBOT',T42,'RMXT',T58,'RMXB')
    WRITE(G,1F0) (1),BTOP(1),BBOT(I),RMXBT(I),RMXBB(1)
    IOIIIAI(IX,I2,T7, F10.3,T23,F10.3,T39,F10.3,T55,F10.3)
    CONIINUE
    (%O TO 155
    ACRVI(1)= XJIOP(1)*Z1(1)
    ACRVB(1)= XJBOT(1)*Z1(1)
    BCRVV(1)= XJTOP(1)*Z2(1)
    BCRVB(I)= XJBOT(1)*Z2(1)
    BCRVB(1)
    Rrixar(i)= XJIOP(1)*2z3(1
    R&MxNB(i)= XJBOM(1)*23(1)
    RPMXIST(1)= XJTOP(1)*ZMI(1
    MMMRBB(1)= XJBOT(1)*Z4(1)
    IF(LEVEL.EQ.3)GO TO 160
    IF(LEVEL.EQ.3)
    IOMHAT(IX,'(I )',T10,'ACRVT',T25,'BCRVT', T40,'RMXAT',T55, 'RMXBT')
    WRIIE(6,170)(I),ACRVT(I),BCRVT(I),RMXAT(I),RMXBT(I)
    WRIIE(6,170)(I),ACRVT(I),BCRVT(I),RMXAT(I),RMXBT(I)
    WRITE (6,175)
    TORRAAI(IX,T10,'ACRVB',T25,'BCRVB',T40,'RMXAB',T55,'RMXBB')
    WRIIE(6,170)(I),ACRVB(I),BCRVB(I),RMXAB(I),RMXBB(I)
    CONTINUE
    GO IO }15
    ACRVT(1)= XJTOP(1)*Z1(1)
    ACRVB(I)= XJBOT(i)*Z1(I)
    BCRVT(1)= Z2(1)
    BCRVB(1)=22(1)
    RMXAT(I)= XJTOP(I)*Z3(1)
    RMXAB(I)= XJBOT(I)*Z3(I)
    IF(IEVEI..EQ.3)GO TO 155
    WRITE (6,180)
    FORMAI(IX,'(I)',T8,'ACRVT',T21, 'BCRVT',T31,'RMXAT',T42,'ACRVB',T
* I,'BCRVB',T66,'RMXAB')
WRITE (6,185)(I), ACRVT(I),BCRVT(I),RMXAT(I),ACRVB(I),BCRVB(I),
* RMXAB(I
FORMAI(IX, I1, T4,F10.3,T16,F10.3, T27, F10.3,T38, F10.3, T49, F10.3,
* TG2,F10.3j)
    GO 10 155
    RMX13I(1)=XJTOP(1)*Z2(1)
    RMX13B(1)=XJBOI(1)*ZZ(1)
    IF (IEVEI.EQ.3) GO TO 155
    WRIIE(6,190)
    IORMAI (IX,I 10,'RMXT',T20,'RMXB')
    IORMAI (IX,I10, RMXT',I20,RMMBB')
    IORMAI(ix,12, T7,F10.3,T17,F10.3)
CONIIPJUE
15
```

```
    KPIXIST(1)= XJTOP(1)*Z1(1)
    FORPAA(IX T10 'ACRVB' T25 'BCRVB' T40 'RMXAB' T55 'RMXBB')
    BCRVB(I)= 22(1)
```

C
READ IN IHE NUHIBER ANID DIMENSIONS OF THE UPPER DECKBOARDS 10 COMPUSE IIIE AVERAGE MOE AND TOTAL MOMENT OF INERTIA
READ（5，200）NODKBD
FORMA1（J30，12）
I．$Y=2$
$1 . P=1$
IL＝
$E A V G=0.0$
ElOT $=0.0$
1FRIIA $=0.0$
101DKS＝0．0
IF（IEVEL．．EQ． 3 ）GO TO 205
WRITE $(6,210)$
IORMAT（／／，14，＇ $140 E^{\prime}$, T20，＇BASE＇，T30，＇DEPTH＇，T45，$\#$ OF BDS＇，T63
＊，＇INERTIA＇）
CONTINUE
READ $(5,75)$
DO $215 \quad i=1$ ，NODKBD
READ $(5,220) E(1), B 1(1), D 1(1), \operatorname{NOBDS}(1)$
FORMAT（T4，F10．1，T32，F5．3，T50，F5．3，T70，12）
ERT I A＝0）． 0
ERTIA＝（（B1（1）＊（D1（1）＊＊3））／12）＊FLOAT（NOBDS（I））
TERTIA＝ERTIA＋TERTIA
ETOI＝E（I）＊FLOAT（NOBDS（I））＋ETOT
TOIDKS＝TOTDKS＋FLOAT（NOBDS（1））
IF（L．EVEL．EQ．3）GO TO 215
WRIIE（6，22）E（1），BI（1），D1（I），NOBDS（I），ERTIA
FORMAT（1X，F10．1，T20，F5．3，T30，F5．3，T49，I2，T61，F10．5）
CONIINUE
FAVG＝ETOT／TOTDKS
If（LEVEL．EQ．3）GO TO 230
WRITE $(6,235$ ）EAVG，TERTIA
FOPMAI（I／＇AVG．MOE＝T11，F10．1，T22，＇PSI＇，T30，＇TOT．MOMENT OF INE

```

```

COHTINUE
IHF FOILOWING ROUTINE BREAKS DOWN THE UNIT I．OAD INTO CERTAIN PIKCENIAGES，ACCORDING TO THE NUMBER OF STRINGERS，AND ALLOCATES TIIEM TO A SIRINGER
READ（5，2l0）NOUNIT
FORMAT（／／，17X，12，／／）

```
```

    IF(LEVEL.EQ.3)GO TO 245
    WIRITE (6,250)NOUNIT
    FORMAT(IX, # OF LOAD CASES= ,T18,12)
    CONTINUE
    IIIIS DO-LOOP COMPUTES THE HMAX FOR VARIOUS UNIT LOADS
    DO 255 IN=1,NOUNIT
    |IMAX=0.0
    XM=0.0
    HLN(IN)=0.0
    Z(IN)=0.0
    Y(IN)=0.0
    RMOM1(IN)=0.0
    RMOM2(IN)=0.0
    RMAXI(IN)=0.0
    RMAX2(IN)=0.0
    RMXT(IN)=0.0
    RHXB(IN)=0.0
    JCT=0
    READ (5,260) UNIT, SPACE, DKL, OHG
    FORMAT (4F10.2)
    IF(LEVEL.EQ. 3)GO TO 265
    FORMAT(//,'LOAD CASE # =',T14,12,T30,'UNIT LOAD= ',T42,F10.3)
    WRITE(6,275)SPACE,DKL,OHG
    HORMAI(1X,'SPACING =''T11,F5.2,T20,'DECK LENGTH =',T33,F5.2,
    * T45,'OVERHANG =',T55,F5.2)
CONTINUE
COMPUIE THE AMOUNT OF UNIT LOAD DISTRIBUTED TO EACH STRINGER

```
```

MI=0

```
MI=0
    M= 0
    M= 0
    IF (NOSTR.EQ.3) GO TO 280
    IF (NOSTR.EQ.3) GO TO 280
    IF (NOSTR.EQ.2) GO TO 285
    IF (NOSTR.EQ.2) GO TO 285
    PB1=0.0
    PB1=0.0
    PB2=0.0
    PB2=0.0
    PB3=0.0
    PB3=0.0
    P[34=0.0
    P[34=0.0
    PB1=SPACE/DKL
    PB1=SPACE/DKL
    PB2= PB1
    PB2= PB1
    PB3=((DKI_2*SPACE)/2)/DKL
    PB3=((DKI_2*SPACE)/2)/DKL
    P131/= PB3
    P131/= PB3
    MI:= NOSTR/4
    MI:= NOSTR/4
    M-M1
```

    M-M1
    ```
\(100 \quad 290 \quad I=1, M\)
\(\mathrm{CON}=\mathrm{M}+\mathrm{I}\)
MI
\(M=M+M 1\)
1)O 295 I=MI,M
\(V(I)=\) UNIT*PB3
CONIINUE
\(M I=M+1\)
\(M \div M+1 \cdot 1\)
\(100 \quad 300 \quad I=M 1, M\)
V(I) =UNIT*PB4
CONIINU
\(M I=M+1\)
\(M=M+M 1\)
\(M=M+M 1\)
DO 305 \(1=111, M\)
V(I):=UNIT*PBZ
CONTINUE
GO TO 310
M1 = NOSTR/3
DO \(315 \quad 1=1\), M
\(V(I)=\) UNITH0. 25
CONT I NUE
\(M I=M+1\)
\(M=M+M 1\)
DO \(320 \quad 1=M 1, M\)
\(V(1)=\) UNIT*0. 5
CONIINUE
\(M I=M+1\)
\(M=M+M 1\)
DO 325 I=M1, M
\(\mathrm{V}(1)=\) UNIT*O. 25
CONTINUE
GO 10310
D0 330 \(1=1,2\)
\(V(1)=0.5^{*}\) UNIT CONTINUE

CONTINUE
IF(LEVEL.EQ. 3)CO TO 335
WRITE 6,3110\()\) OKL
FORMAT( \(/ /{ }^{\prime}\) 'DECKBOARD(S) LENGTH \(=\) ',F4.1,T28,'IN.') WRITE (6,345)
IORMAI (IX,' SIRINGER', T25, 'APPLIED LOAD')
DO \(335 I=1\), NOSTR
WRITE (6,350)I,V(I)
TORMAT(1X, T4, 12, T26,F10.3)

CONTINUE
TRICT= 0.55
H1OI \(=0.0\)
11 in \(1 T=0.00\)
If (JOP.EQ.1) GO TO 365
DO) \(370 \quad i=1\), NOSTR
IIINIT= IIINIT +V(I)*W(I)/(2.0*D(I))
COMTINUE
G() TO 375
DO \(380 \quad I=1\), NOSTR
HINIT= HINIT + V(I)*W(I)/(2.0*D(1))
CONI INUE
\(00385 \mathrm{I}=1\), NOSIR
IINIT= HINIT + FRICT*V(I)*VOF/(D(I)-VOF)
COHTINUE
385
C
315
\(3 / 5\)
VARIABLES FOR K-FACTOR REGRESSION EQUATIONS
\(\times 1=0.0\)
\(\times 5=0.0\)
\(\times 6=0.0\)
\(\times 7=0.0\)
\(\times 8=0.0\)
\(\times 10=0.0\)
IF (NOSTR.EQ. II) GO 10355
X1=UNIT
X8=SPACE**3
Y7 = TERTIA*E.AVG
xゥ=(W(1)+W(2)+W(3))/3.
\(X 6=D(1)\)
co 10360
XII = UN I T
X8=((DKL-SPACE)/2)**3
\(\times 10=\) TERTIA*EAVG
\(\times 6=D(1)\)
\(\times 7=(W(1)+W(2)+W(3)+W(4)) / 4\).

\section*{FSIABLISII INITIAL PARAMETERS. INCLUDING FRICTION RESISTANCE FOR} SIIGIE-FACED PALLETS IN 'HINIT'

CONTINUE

IIIIS SECIION PRODUCES A PICTURE OF THE PALLET DESIGN WITH III：UNIT LOAD AND IIINIT APPLIED

IF（IEVEL．GT．O）GO TO 390
WRITE \((6,395)\) UNIT

＊lilv）
```

FORMAT 6，100）HINIT
＊7（1H1－） $\mathrm{J}^{\prime}$ INITIAL IIORZ．FORCE $={ }^{\prime}, 1 \mathrm{X}, \mathrm{F} 7.1,1 \mathrm{X},{ }^{\prime}$ LBS＇，T37，

```

If NOSTR FQ 4 i
IF（NOSTR．EQ．2）GO TO 410
WIRITE（6，415）
FORMAI（T45，＇＊＇，T61，＇＊＇，T76，＇＊＇）
WRITE \((6,415)\)
CO TO 1120
WRITE（6，1，25
FORMAT（T45，＊＇，T55，＇＊＇，T66，＇＊＇，T76，＇＊＇）
WRITE（6．425）
WRITE \((6,425)\)
WRITE \((6,425)\)
GO \(10 \quad 120\)
CONTINUE
FORMAI（145，＇＊＇，T76，＇＊＇）
VRITE 6.430 ）
WRITE（6，430）
IF（JOP．ER．1）GO TO 435
WRITE 6，14 40 ）
FORHAT（T45，32（1 \(\left.\mathrm{H}^{*}\right)\) ）
GO 10 LIIS
IF（NOSIR．EQ．4）GO TO 450
IF（MOSTR．EQ．2）GO 10455
WRIIE \((6,415)\)
GO TO 390
WRIIE \((6,1125)\)
IF（NOSIR．EQ．3）GO 10390
WRITE（6，460），
FORMAT（I5＇5，＇j＇，166，＇ 1 ＇）
WRITE \((6,465)\) SPACE
FORMAI（T55，＇SPACING \(=\)＇，F5．2，T71，＇IN．＇）
（G） 10390
WIRIJE（6，1430）

COMPUTE VAIUES AT EACH INCREMENT
\(x=0.0\)
PSI: 0.0
IIIETA \(=0.0\)
IIE IA \(2=0.0\)
AL.PHA \(=0.0\)
\(A L P H A 2=0.0\)
PSI2=0.0
MNUF \(=0\)
NJPM=:0
\(E N T C P T=0.0\)

IN IHIS DO-LOOP HTOT IS COMPUTED AT EACH XINC

DO \(\begin{gathered}170 \\ x=x+x I N C\end{gathered}\)
\(x=x+X I N C\)
\(H T O T=0.0\)

IN THIS DO-LOOP H IS COMPUTED FOR EACH STRINGER AT EACH XINC

DO \(475 K=1\), NOSTR
R1=0.0
\(R 2=0.0\)
YM 0.0
\(\operatorname{PSI}=(\operatorname{ATAN}(D(K) / W(K))) * 57.296\)
\(\operatorname{IILN}(K)=\operatorname{SQRT}(D(K) * * 2+W(K) * * 2)\)
\(Z(K)=W(K)-X\)
YM=SQR1 (HILN \((K) * * 2-Z(K) * * 2)\)
AI. PHA \(=(\) ARS IN \((Y M / H L N(K))) * 57.296\)
THETA=ALPHA-PSI
PSI2=90.0-PSI
AL. PHA2 \(=90.0-\) ALPHA
TIIETA2=PSI2-ALPHA2
TN: O. O
\(T N=W(K)-V O F *\) TAN(THETA2/57.296)
IF (X.GE.TN)GO TO 485
GO 101180
\(Z(K)=W(K)-X\)
YM=SQRT(IILN(K)**2-Z(K)**2)
AI PHA=90.0+90.0-( (ARSIN(YM/HLN(K)))*57.296)
THETA=AI PHA-PSI
THETAZ = THETA
ALPHA2 \(=0.0\)
IF(JP(K).NE.O) GO TO 490 MNUM=1
\(N J I M=2\)
IF(JP(K).NE. 1 ) GO TO 495 MNUM=: 1
```

                            IF(JP(K).NE.2) GO TO 500
        MNUM=2
        IF(JP(K).NE.3) GO TO 505
        MNUM=3
        HJPPM=4
    IN THIS DO-LOOP THE TOTAL ROTATION MODULUS FOR THE TOP AND
    BOIIOM JOINT ALONG A SIRINGER IS COMPUTED
    DO 510 M=MNUM, NJPM
        THICR1=0.0
            THTCR2=0.0
            ENTCPT=0.0
            1H[ICR=0.0
            IF(IIJT(M).EQ.1)GO TO 515
            IF (NJT(M), EQ. 3)GO TO 520
            TIHTCR1 = (RAMXAT (M) +RMXAB(M) *57.296/( ACRVT (M)+ACRVB(M))
            ENTCPT = (RMXAT(M) +RMXAB(M))/((BCRVT(M)+BCRVB(M))*
            (THTCR1/57.296))
            l
            +BCRVB(M))
            GO TO 525
            THE 1CR=((RMXAT(M)+RMXAB(M))/(ACRVT (M)+ACRVB(M)))
            **(1.0/(BCRVT(M)))*57.296
            GO JO 525
            THF:ICR=(RMXBT(M)+RMXBB(M) )*57.296/(BTOP(M)+BBOT (M))
            IF (NJT(M).EQ.3)GO TO 530
            IF (NJT(M).EQ.1)GO TO 535
            IF (THETA.I.E.THTCR1)GO TO 540
            IF (THETA.LE.THTCR2)GO TO 545
            RMOH11(M) =RMXBT(M)
            RMOH1(M)=RMXBI(M)
            MMOM2(M)=
            RMOH11(M) = (BCRVT (M)*THETA/57.296) + ENTCP
            RMOH1(M)=(BCRVJ(M)*THETA/57.296)+ENTCPT
            RMOH2(M)=(BCRVB(M)*THETA/57.296) + ENTCPT
            G0 10 550
            RMOH11(M)=ACRVT (M)*THETA/57.296
            RMOM2 (M)=ACRVB(M)* THETA/57.296
            GO IO 550
            RMOH11 (H)=BTOP (M)*THETA/57.296
            RMOHIZ(M) = BBOT(M)* THETA/57.296
            IF(TIIETA.CE. THE TCR RMOM1 (M)=RMXBT(M)
            II( IIIE TA.GE.THETCR )RMOM2(M)=RMXBB(M)
            CO TO 55O
            RMOM1(M)=ACRVT(M)*(THETA/57.296)**BCRVT(M)
            RMOHI2(M)=ACRVB(H)*(IHETA/57.296)**BCRVB(M)
            If (IHEIA.GE.THETCR)RHOM1(M)=RMXAT(M)
    ```

\section*{If(TIIE TA.GE.THETCR)RMOM2(M)=RMXAB(M)}

\(R 1=R 1+R M O H 1(M)\)
\(R 2=R 2+R M O M 2(M)\)
IF(LEVEL.GT.0) GO TO 510
WRIIE(G,555)R1,R2,(M)
IORPHAI(1X,2F10.3,T30,11)
COHTIHUE

\section*{\(R M_{M A} \times 1(K)=R 1\) \\ RHAK2 (K)=R2}

IF(IEVEL.GI.O) GO TO 560
WRI IE \((6,565)\) AL. PHA, ALPIIA2, PSI 2, YM, Z (K), THTCR1
FORMAI (1X, GF13.6)
URITE \((6,565)\) THETCR, PSI, THETA, THETA2, ENCPT, THTCR2
WRIIE( 6,570 ) RMAXI (K), RMAX2 (K)
FOIRMAT (1X, 2F15.3)
\(C A=0.0\)
CR=0.0
If (NOSTR.EQ.2) GO TO 575
IF (NOSIR.EQ.3) GO TO 580

FOIJR SIRINGFR REGRESSION EQUATION

CA=0.13057599-0.00001176*×1+0.04938176*×10/×8-0.05689698*X7/X6-0.00002484* (RMXBT (1) +RMXBB(1)) GO 10585

IIIKEE SIRIMGER REGIRESSION EQUATION
* \(\mathrm{CA}=0.89561928+0.0003172^{*} \times 1+0.00130390^{*} \times 7 / \times 8-1.60039455^{*} \times 5 / \times 6\) +. 00006912*(RMXBB(1) +RMXBT(1))
GO 10585

TWO STRIHGER EQUATIONS
\(R Y=0.0\)
RW:=0.0
RY: = ( (INNIT/(SPACE+2*OHG))* (SPACE**3))/(24*EAVG*TERTIA) RW~ ((IINII/(SPACE+2*OHG))*OHG**2*SPACE)/(4*EAVG*TERTIA) ALPHA: AL PIIA/57. 296
```

$B A=(A I P \| \Lambda-R Y+R W) / A L P H A$
$R R=(A L . P H A+R Y-R W) / A L P H A$
F（K．EQ．1）CUR＝CA
I（K．EQ． 2 ）CUR $=C R$
IF（CUR．GT．1．0）CUR＝1．0
IF（CUR．LE．O．O）CUR＝0．0
IITOT $=11101+\left((V(K) *(T N-X))+C U R * R M A X 1(K)+R M A X 2(K)-\left(.55^{*} V(K) * V O F\right.\right.$
）／（YM－VOF
010475

```

IF（CA．GT．1．0）\(C A=1.0\)
IF（CA．LE．O．O）\(C A=0.0\)
11 OOT \(=11 T O T+\left((V(K) *(T N-X))+C A^{*}\left(\operatorname{RMAX1}(K)+\operatorname{RMAX2(K))-(.55^{*}V(K)*VO}\right.\right.\)
＊））／（YM－VOF）
（F（LEVEI．GI．O）GO TO 475
WRITE（6，590）X，K，HTOT
FORMAT（1X，F6．4，111，F21．3）
CONTINUE

If THE NEXT 18 LINES HMAX，AND THE CORRESPONDING ROTATION MODULI AND XINC ARE FILED
\(\operatorname{HS}(J)=H T O T\)
\(x S(J)=x\)
If（HTOT．LE．HMAX）GO TO 593
IIIAAX＝HTOT
XI \(=\mathrm{X}\)
DO 600 I＝\(=1\) ，NOSTR
\(\operatorname{RMXT}(L)=\operatorname{RMAX1}(L)\)
\(\operatorname{RMXB}(L)=\operatorname{RMAX2(L)}\)

CONTINUE
GO 10470
If（JCT．EQ．20）GO TO 595
C
\(C\)
170
\(\stackrel{C}{C}\)
C
\(\therefore\)
らの「

\section*{COHTINUE}

COHPUIE H／V RATIO
（11）－1）． 0
\(\mathrm{VHI}=1.0\)
IIU＝IIMAX／UN I T
TIII SECTION PRODUCES A PICTURE WITH THE UNIT LOAD ON A IISPIACED PAILET．ALSO，THE H／V RATIO
IF（IEVEL．EQ．3）GO 10255
WRIIE \((6.605)\) UNIT
```



```
＊IIV）！
WRIIE（6．610）IIMAX
FORMAT（ \(/, \mathrm{T} 5,{ }^{\prime}{ }^{\prime}\) HMAX \(={ }^{\prime}, 1 \mathrm{X}, \mathrm{F} 7.1,1 \mathrm{~K},{ }^{\prime}\) LBS＇， \(\left.5 \mathrm{X}, 10(1 \mathrm{H}-)^{\prime},^{\prime}\right)^{\prime}, \mathrm{T} 39,32\left(1 \mathrm{H}^{*}\right.\)
＊1）
IF（NOSTR．EQ．4）GO 10615
F（NOSTR．EQ．2）GO TO 620
WRIJE（6．625
FORMAT（ T 36, ＊＇\(^{\prime}\) ，T52，＇＊＇，T68，＇＊＇）
CO IO 627
WRITE \((6,630)\)
```



```
GO 「O 627
IRITE \((6,635)\)
IORMAI（ix，T36，＇＊＇，T68，＇＊＇）
GO IO 627
IF（JOP．EQ．1）GO TO 650
WRITE（ 6,640 ）
FORMAT（T33，33（1H＊））
GO 10645
IF（NOSTR．EQ．4）GO TO 655
FF（NOSIR．EQ．2）GO TO 660
WRITE 6,665
TORMAI（i33，＊＇，T49，＇＊＇，T65，＇＊＇）
GO TO 645
WRIIE \((6,670)\)
FORMAT（＇ 33, ＊＇\(^{\prime}\), T43，＇＊＇，T55，＇＊＇，T65，＇\({ }^{\prime \prime}\)＇）
GO 10645
WRITE（6，675）
133＇＊＇，T65，＇＊＇
F（NOSTR．NE．4）GO TO 645
WIRITE \((6,680)\)
TORMAT（ix，T46，＇I＇，T58，＇I＇）
WRITE 6.685\()\) SPACE
IORMAI（i46，SPACING＝＇，F5．2，T71，＇IN＇）
WRITE（6．690）
ORMAT（ \(\left.165, I^{\prime}, T 70,1 I^{\prime}\right)\)
TRIIE \((6,695) \mathrm{XM}\)
ORMAT（T67，XM \(=\)＇，1X，F5．3，1X，＇IN＇）
WRIJE（6，700）HU
FORMAI（1X，＇HMAX／UNIT \(=1\), T14，F8．5）
OUIPUT MOMENIS GENERATED ALONG EACH STRINGER
```

```
|O; VRIIE(G,70';)
        IORMA1(//, VALUCS OF MOM
        WRITE (6,715)
        FORMAT (1X,15,'StRINGER H',T25,'tOP MOMENT')
        GO 10 720
        WRITE. (6,725)
        FORMAI (1x,T5,'STRINGER #',T25,'TOP MOMENT',T45,'BOTTOM MOMENT')
        DO }730\quad1=1\mathrm{ , NOSIR
            WRITE (6,735) (1),RMAXI(1),RMAX2(1)
        FORMA1 (iX,T10.11,T25,F10.3,T45,F10.3)
        CONIINUE
        CO 10 740
        DO 745 I=1, NOSTR
        WRITE (6,750) (1), RMXT(1)
        TORIMAT (ix,T10,11,T25,F10.3)
        CONTINUE
        contifuE
    CALCULAIION OF WORK UP TO HMAX. WORK IS THE AREA UNDER THE X-HTOT
    CuRVE
    WRITE(6,755)
    WRITE (6,760)
    FORMAI(IX,T2,'XINC',T23,'WORK')
    XMAXN=0.0
XR=0.0
AREA1=0.0
AREA2=0.0
XR1=0.0
AR1=0.0
AR2=0.0
AR3=0.0
NMAX=(XM/XINC)+1
XR=|S(1)-HINIT
AREA1=(XR*XINC)/2
ARFAZ=HINIT*XINC
AREAL HINIT*XINC
DO 765 I=2,NMAX
    XRI=HS(1)-HS(1-1)
    AR1=(XR1* XINC)/2
    AR2=HS(1-1)*XINC
    AR3=AR1 +AR2+AR3
    VRIIE (6,770)XS(1),AR3
    FORMAT (1X,F1O.5,F20.3)
```

$2!$
$C$
$C$
SIOP
OEBIJG UNIT(6), SUBCHK, SUBTRACE
END
CONTINUE
CONTINUE

B2 - Analog Models

FIGURE B2.2-Four Stringer Analog Model

B3 - Pallet Designs for Computer

Table B3.1. Three Stringer, Double-Faced Pallets Designed for K-Factor Developement

| $E I / L^{3}$ (lb./in.) | Stringer Aspect Ratio (in./in.) | $\begin{aligned} & \text { Joint } \\ & \text { Characteristics } \end{aligned}$ |  |
| :---: | :---: | :---: | :---: |
| 1675.0 | 0.27 | 100 | 1000 |
| 167.9 | 0.27 | 100 | 1000 |
| 9.9 | 0.27 | 100 | 1000 |
| 1675.0 | 0.43 | 100 | 1000 |
| 167.9 | 0.43 | 100 | 1000 |
| 9.9 | 0.43 | 100 | 1000 |
| 1675.0 | 0.58 | 100 | 1000 |
| 167.9 | 0.58 | 100 | 1000 |
| 9.9 | 0.58 | 100 | 1000 |
| 1675.0 | 0.27 | 250 | 5500 |
| 167.9 | 0.27 | 250 | 5500 |
| 9.9 | 0.27 | 250 | 5500 |
| 1675.0 | 0.43 | 250 | 5500 |
| 167.9 | 0.43 | 250 | 5500 |
| 9.9 | 0.43 | 250 | 5500 |
| 1675.0 | 0.58 | 250 | 5500 |
| 167.9 | 0.58 | 250 | 5500 |
| 9.9 | 0.58 | 250 | 5500 |
| 1675.0 | 0.27 | 400 | 10000 |
| 167.9 | 0.27 | 400 | 10000 |
| 9.9 | 0.27 | 400 | 10000 |
| 1675.0 | 0.43 | 400 | 10000 |
| 167.9 | 0.43 | 400 | 10000 |
| 9.9 | 0.43 | 400 | 10000 |
| 1675.0 | 0.58 | 400 | 10000 |
| 167.9 | 0.58 | 400 | 10000 |
| 9.9 | 0.58 | 400 | 10000 |

${ }^{1}$ Characteristics given are 1. $M_{\max }$ (in.-1b.)
2. R (in.-lb./radian)

Table B3.2. Four Stringer, Double-Faced Pallets Designed for K-Eactor Developement

| $E I / L^{3}$ $(l b . / i n$. | Stringer Aspect Ratio (in./in.) | ```Joint Characteristics'``` |  |
| :---: | :---: | :---: | :---: |
| 631.0 | 0.27 | 100 | 1000 |
| 85.9 | 0.27 | 100 | 1000 |
| 6.6 | 0.27 | 100 | 1000 |
| 631.0 | 0.43 | 100 | 1000 |
| 85.9 | 0.43 | 100 | 1000 |
| 6.6 | 0.43 | 100 | 1000 |
| 631.0 | 0.58 | 100 | 1000 |
| 85.9 | 0.58 | 100 | 1000 |
| 6.6 | 0.58 | 100 | 1000 |
| 631.0 | 0.27 | 250 | 5500 |
| 85.9 | 0.27 | 250 | 5500 |
| 6.6 | 0.27 | 250 | 5500 |
| 631.0 | 0.43 | 250 | 5500 |
| 85.9 | 0.43 | 250 | 5500 |
| 6.6 | 0.43 | 250 | 5500 |
| 631.0 | 0.58 | 250 | 5500 |
| 85.9 | 0.58 | 250 | 5500 |
| 6.6 | 0.58 | 250 | 5500 |
| 631.0 | 0.27 | 400 | 10000 |
| 85.9 | 0.27 | 400 | 10000 |
| 6.6 | 0.27 | 400 | 10000 |
| 631.0 | 0.43 | 400 | 10000 |
| 85.9 | 0.43 | 400 | 10000 |
| 6.6 | 0.43 | 400 | 10000 |
| 631.0 | 0.58 | 400 | 10000 |
| 85.9 | 0.58 | 400 | 10000 |
| 6.6 | 0.58 | 400 | 10000 |

[^0]Table B3.3. Three Stringer, Single-Faced Pallets Designed for K-Factor Developement

| $\begin{gathered} E I / L^{3} \\ (l b . / i n .) \end{gathered}$ | Stringer Aspect Ratio (in./in.) | ```Joint Characteristics' M max R``` |  |
| :---: | :---: | :---: | :---: |
| 1675.0 | 0.58 | 400 | 10000 |
| 1675.0 | 0.43 | 400 | 10000 |
| 1675.0 | 0.27 | 400 | 10000 |
| 1675.0 | 0.58 | 250 | 5500 |
| 1675.0 | 0.58 | 100 | 1000 |
| 167.9 | 0.43 | 400 | 10000 |
| 167.9 | 0.58 | 250 | 5500 |
| 9.9 | 0.58 | 250 | 10000 |
| 9 |  |  | 10000 |

${ }^{1}$ Characteristics given are 1. $M_{\max }$ (in.-1b.)
2. $R$ (in.-lb./radian)

Table B3.4. Four Stringer, Single-Faced Pallets Designed for K-Factor Developement

| $E I / L^{3}$ $(l b / i n$. | Stringer Aspect Ratio (in./in.) | ```Joint Characteristics'``` |  |
| :---: | :---: | :---: | :---: |
| 631.0 | 0.58 | 400 | 10000 |
| 631.0 | 0.43 | 400 | 10000 |
| 631.0 | 0.27 | 400 | 10000 |
| 631.0 | 0.58 | 250 | 5500 |
|  |  |  |  |
| 8.6 | 0.43 | 400 | 10000 |
|  |  |  |  |
| 8.6 | 0.58 | 250 | 5500 |
| 6.6 | 0.58 | 250 | 10000 |
|  |  |  |  |

${ }^{1}$ Characteristics given are 1. $M_{\max }$ (in.-lb.)
2. R (in.-1b./radian)

## APPENDIX C

C1 - Fastener Patterns
C2 - Construction Specifications and Unit Load for Type I Pallets

C3 - Construction Specifications for Joint Rotation Samples C3.1 - Specification of Joint Rotation Samples Fastened with Nails

C3.2 - Specification of Joint Rotation Samples Fastened with Staples

C3.3 - Specification of Joint Rotation Samples for Rate of Loading Study

C4 - Upper Deckboard MOE by Pallet
C5 - Construction Specifications and Unit Load for Type II Pallets

C6 - Construction Specifications and Unit Load for Field Pallets

C1 - Fastener Patterns

FIGURE C1.1 - Nail Patterns


FIGURE C1.2 - Staple Patterns

C2 - Construction Specifications and Unit Load for Type I Pallets

Table C2. Construction Specificatons and Unit Loads Applied During Type I Testing

(1) All dimension in inches

C3 - Construction Specifications for Joint Rotation Samples

Table C3.1 Specifications of Joint Rotation Samples Eastened with Nails ${ }^{1}$

| Specimen No. | Deckboard |  | Stringer |  | Fastener |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Width | Thickness | Width | Height | \# | Type |
| 1 | 6.5 | 0.5 | 1.5 | 3.5 | 4 | Nail |
| 2 | 6.5 | 0.5 | 1.5 | 3.5 | 4 | Nail |
| 3 | 6.5 | 0.5 | 1.5 | 3.5 | 4 | Nail |
| 4 | 6.5 | 0.5 | 1.5 | 3.5 | 3 | Nail |
| 5 | 6.5 | 0.5 | 1.5 | 3.5 | 3 | Nail |
| 6 | 6.5 | 0.5 | 1.5 | 3.5 | 3 | Nail |
| 7 | 3.5 | 0.375 | 1.5 | 3.5 | 2 | Nail |
| 8 | 3.5 | 0.375 | 1.5 | 3.5 | 2 | Nail |
| 9 | 3.5 | 0.375 | 1.5 | 3.5 | 2 | Nail |
| 10 | 5.5 | 0.5 | 1.5 | 3.5 | 1 | Nail |
| 11 | 5.5 | 0.5 | 1.5 | 3.5 | 1 | Nail |
| 12 | 5.5 | 0.5 | 1.5 | 3.5 | 1 | Nail |

1 All dimensions in inches

Table C3.2 Specifications of Joint Rotation Samples Fastened with Staples ${ }^{2}$

| Specimen No. | Deckboard |  | Stringer |  | Fastener |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Width | Thickness | Width | Height | \# | Type |
| 1 | 5.0 | 0.5 | 1.5 | 3.5 | 4 | Staple |
| 2 | 5.0 | 0.5 | 1.5 | 3.5 | 4 | Staple |
| 3 | 5.0 | 0.5 | 1.5 | 3.5 | 4 | Staple |
| 4 | 5.0 | 0.5 | 1.37 | 3.5 | 3 | Staple |
| 5 | 5.0 | 0.5 | 1.37 | 3.5 | 3 | Staple |
| 6 | 5.0 | 0.5 | 1.37 | 3.5 | 3 | Staple |
| 7 | 5.0 | 0.5 | 1.13 | 3.5 | 2 | Staple |
| 8 | 5.0 | 0.5 | 1.13 | 3.5 | 2 | Staple |
| 9 | 5.0 | 0.5 | 1.13 | 3.5 | 2 | Staple |
| 10 | 5.0 | 0.5 | 1.37 | 3.5 | 1 | Staple |
| 11 | 5.0 | 0.5 | 1.37 | 3.5 | 1 | Staple |
| 12 | 5.0 | 0.5 | 1.37 | 3.5 | 1 | Staple |

${ }^{1}$ All dimensions in inches

Table C3. 3 Specifications of Joint Rotation Samples For Rate of Loading Study ${ }^{1}$

| Specimen No. | Deckboard |  | Stringer |  | Fastener |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Width | Thickness | Width | Height\| | \# | Type |
| 1 | 6.5 | 0.5 | 1.5 | 3.5 | 4 | Nail |
| 2 | 6.5 | 0.5 | 1.5 | 3.5 | 4 | Nail |
| 3 | 6.5 | 0.5 | 1.5 | 3.5 | 4 | Nail |
| 4 | 6.5 | 0.5 | 1.5 | 3.5 | 4 | Nail |
| 5 | 6.5 | 0.5 | 1.5 | 3.5 | 4 | Nail |
| 6 | 6.5 | 0.5 | 1.5 | 3.5 | 4 | Nail |
| 7 | 6.5 | 0.5 | 1.5 | 3.5 | 4 | Nail |
| 8 | 6.5 | 0.5 | 1.5 | 3.5 | 4 | Nail |
| 9 | 6.5 | 0.5 | 1.5 | 3.5 | 3 | Nail |
| 10 | 6.5 | 0.5 | 1.5 | 3.5 | 3 | Nail |
| 11 | 6.5 | 0.5 | 1.5 | 3.5 | 3 | Nail |
| 12 | 6.5 | 0.5 | 1.5 | 3.5 | 3 | Nail |
| 13 | 6.5 | 0.5 | 1.5 | 3.5 | 3 | Nail |
| 14 | 6.5 | 0.5 | 1.5 | 3.5 | 3 | Nail |
| 15 | 6.5 | 0.5 | 1.5 | 3.5 | 3 | Nail |
| 16 | 6.5 | 0.5 | 1.5 | 3.5 | 3 | Nail |
| 17 | 5.0 | 0.5 | 1.37 | 3.5 | 3 | Staple |
| 18 | 5.0 | 0.5 | 1.37 | 3.5 | 3 | Staple |
| 19 | 5.0 | 0.5 | 1.37 | 3.5 | 3 | Staple |
| 20 | 5.0 | 0.5 | 1.37 | 3.5 | 3 | Staple |
| 21 | 5.0 | 0.5 | 1.37 | 3.5 | 3 | Staple |
| 22 | 5.0 | 0.5 | 1.37 | 3.5 | 3 | Staple |
| 23 | 5.0 | 0.5 | 1.37 | 3.5 | 3 | Staple |
| 24 | 5.0 | 0.5 | 1.37 | 3.5 | 3 | Staple |
| 25 | 5.0 | 0.5 | 1.37 | 3.5 | 1 | Staple |
| 26 | 5.0 | 0.5 | 1.37 | 3.5 | 1 | Staple |
| 27 | 5.0 | 0.5 | 1.37 | 3.5 | 1 | Staple |
| 28 | 5.0 | 0.5 | 1.37 | 3.5 | 1 | Staple |
| 29 | 5.0 | 0.5 | 1.37 | 3.5 | 1 | Staple |
| 30 | 5.0 | 0.5 | 1.37 | 3.5 | 1 | Staple |
| 31 | 5.0 | 0.5 | 1.37 | 3.5 | 1 | Staple |
| 32 | 5.0 | 0.5 | 1.37 | 3.5 | 1 | Staple |

${ }^{1}$ All dimensions in inches

Table C4. Upper Deckboard MOE by Pallet

| Pallet No. | Species | $\begin{aligned} & \text { MOE } \\ & \text { PSIX10' } \end{aligned}$ | Average MOE PSIx10 ${ }^{6}$ |
| :---: | :---: | :---: | :---: |
| 1 | Aspen | 1.10 | 1.17 |
|  |  | 1.14 |  |
|  |  | 1.15 |  |
|  |  | 1.18 |  |
|  |  | 1.16 |  |
|  |  | 1.28 |  |
| 2 | Aspen | 1.34 | 1.33 |
|  |  | 1.30 |  |
|  |  | 1.30 |  |
|  |  | 1.32 |  |
|  |  | 1.33 |  |
|  |  | 1.33 |  |
|  |  | 1.40 |  |
| 3 | Aspen | 1.16 | 1.18 |
|  |  | 1.16 |  |
|  |  | 1.17 |  |
|  |  | 1.18 |  |
|  |  | 1.18 |  |
|  |  | 1.22 |  |
| 4 | Aspen | 1.20 | 1.23 |
|  |  | 1.23 |  |
|  |  | 1.30 |  |
|  |  | 1.22 |  |
| 5 | Aspen | 1.13 | 1.09 |
|  |  | 1.05 |  |
|  |  | 0.98 |  |
|  |  | 0.99 |  |
|  |  | 1.10 |  |
|  |  | 1.10 |  |
|  |  | 1.04 |  |
|  |  | 1.35 |  |
| 6 | Aspen |  | 0.99 |
|  |  | 0.99 |  |
|  |  | 0.98 |  |
|  |  | 0.99 |  |

Table C4. Upper Deckboard MOE by Pallet, Continued

| Pallet No. | Species | $\begin{gathered} \text { MOE } \\ \text { PSIX10' } \end{gathered}$ | Average MOE PSIx10 ${ }^{6}$ |
| :---: | :---: | :---: | :---: |
| 7 | Oak | $\begin{aligned} & 0.93 \\ & 0.94 \\ & 0.94 \\ & 0.94 \end{aligned}$ | 0.94 |
| 8 | Aspen | $\begin{aligned} & 0.95 \\ & 1.03 \\ & 0.97 \\ & 0.93 \end{aligned}$ | 0.97 |
| 9 | Aspen | $\begin{aligned} & 1.31 \\ & 1.38 \\ & 1.40 \\ & 1.36 \\ & 1.39 \\ & 1.37 \\ & 1.41 \end{aligned}$ | 1.37 |
| 10 | Oak | $\begin{aligned} & 1.45 \\ & 1.48 \\ & 1.50 \\ & 1.46 \\ & 1.43 \\ & 1.50 \end{aligned}$ | 1.47 |
| 11 | Oak | $\begin{aligned} & 1.00 \\ & 0.96 \\ & 0.99 \\ & 0.98 \\ & 0.98 \\ & 0.98 \end{aligned}$ | 0.98 |
| 12 | Oak | $\begin{aligned} & 1.53 \\ & 1.56 \\ & 1.60 \\ & 1.54 \\ & 1.55 \\ & 1.53 \\ & 1.53 \\ & 1.52 \end{aligned}$ | 1.55 |

Table C4. Upper Deckboard MOE by Pallet, Continued

| Pallet No. | Species | $\begin{aligned} & \text { MOE } \\ & \text { PSI×10' } \end{aligned}$ | Average MOE PSIx10 ${ }^{6}$ |
| :---: | :---: | :---: | :---: |
| 13 | Oak | 1.58 | 1.48 |
|  |  | 1.41 |  |
|  |  | 1.48 |  |
|  |  | 1.50 |  |
|  |  | 1.41 |  |
|  |  | 1.49 |  |
| 14 | Aspen | 1.23 | 1.26 |
|  |  | 1.28 |  |
|  |  | 1.18 |  |
|  |  | 1.31 |  |
|  |  | 1.26 |  |
|  |  | 1.29 |  |
| 15 | Oak | 1.40 | 1.39 |
|  |  | 1.41 |  |
|  |  | 1.37 |  |
|  |  | 1.39 |  |
|  |  | 1.37 |  |
|  |  | 1.39 |  |
| 16 | Oak | 1.36 | 1.38 |
|  |  | 1.40 |  |
|  |  | 1.38 |  |
|  |  | 1.33 |  |
|  |  | 1.33 |  |
|  |  | 1.31 |  |
|  |  | $1.41$ |  |
|  |  | 1.51 |  |
| 17 | Oak |  | 1.10 |
|  |  | 1.10 |  |
|  |  | 1.07 |  |
|  |  | 1.10 |  |
|  |  | 1.15 |  |
| 18 | Oak |  | 1.24 |
|  |  | 1.25 |  |
|  |  | 1.24 |  |
|  |  | 1.23 |  |
|  |  | 1.27 |  |

C5 - Construction Specifications and Unit Load for Type II Pallets

Table C5. Construction Specifications and Unit Loads Applied During Type II Testing

(1) All dimensions in inches

C6 - Construction Specifications and Unit Load for Field Pallets

Table C6. Specifications of Designs Found During field Survey

(1) Includes all available information
(2) All dimensions in inches

Table C6. Specifications of Designs Found During Field Survey (continued)

(1) Includes all available information
(2) All dimensions in inches

## APPENDIX D

D1 - Result of Joint Rotation Tests
D1.1 - Test Results of Joint Rotation Samples for Nails
D1.2 - Test Results of Joint Rotation Samples for Staples

D1.3 - Test Results of Joint Rotation Samples for Rate of Loading Study

D2 - Regression Equations for Individual Joints
D2.1 - K-factor Regression Equations and Corresponding R-Square Values for 3 Stringer Single-faced Pallets

D2.2 - K-factor Regression Equations and Corresponding R-Square Values for 3 Stringer Double-faced Pallets

D2.3 - K-factor Regression Equations and Corresponding R-Square Values for 4 Stringer Single-faced Pallets

D2.4 - K-factor Regression Equations and Corresponding R-Square Values for 4 Stringer Double-faced Pallets

D1 - Result of Joint Rotation Tests

Table D1.1 Test Results of Joint Rotation Samples for Nails

| Joint No. | Deckboard |  | Stringer |  | RotationModulus(in-lb/radian) | Mmax Actual (in-ib) | $\begin{gathered} \text { Mmax } \\ \text { Predicted } \\ (i n-l b) \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | MC (\%) | G | MC (\%) | G |  |  |  |
| 1 | 31 | . 71 | 31 | . 69 | 4650 | 660 | 643 |
| 2 | 28 | . 69 | 30 | . 66 | 5575 | 785 | 543 |
| 3 | 30 | . 65 | 30 | . 63 | 4775 | 655 | 543 |
| 4 | 31 | . 63 | 32 | . 64 | 4870 | 555 | 350 |
| 5 | 30 | . 63 | 29 | . 61 | 5210 | 630 | 350 |
| 6 | 30 | . 62 | 33 | . 65 | 4920 | 765 | 420 |
| 7 | 33 | . 69 | 34 | . 63 | 9870 | 343 | 378 |
| 8 | 36 | . 63 | 35 | . 62 | 11210 | 515 | 295 |
| 9 | 34 | . 64 | 34 | . 64 | 8900 | 342 | 284 |
| 10 | 32 | . 64 | 30 | . 60 | 4995 | 175 | 260 |
| 11 | 32 | . 67 | 37 | . 65 | 6210 | 248 | 247 |
| 12 | 35 | . 66 | 36 | . 66 | 5295 | 327 | 263 |

Table D1.2 Test Results of Joint Rotation Samples for Staples

| Joint No. | Deckboard |  | Stringer |  | Rotation Modulus (in-lb/radian) | Mmax Actual$(i n-1 b)$ | Mmax <br> Predicted $(i n-1 b)$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\begin{aligned} & \hline M C \\ & (\%) \end{aligned}$ | G | $\begin{aligned} & \hline M C \\ & (\%) \end{aligned}$ | G |  |  |  |
| 1 | 31 | . 38 | 11 | . 41 | 2704 | 256 | 187 |
| 2 | 37 | . 32 | 12 | . 34 | 2910 | 210 | 218 |
| 3 | 30 | . 35 | 13 | . 39 | 2790 | 197 | 133 |
| 4 | 40 | . 30 | 12 | . 42 | 1874 | 125 | 117 |
| 5 | 40 | . 36 | 13 | . 36 | 2190 | 165 | 186 |
| 6 | 32 | . 31 | 11 | . 38 | 1936 | 175 | 210 |
| 7 | 36 | . 40 | 12 | . 40 | 845 | 64 | 52 |
| 8 | 40 | . 30 | 12 | . 42 | 1250 | 92 | 117 |
| 9 | 30 | . 35 | 13 | . 39 | 905 | 144 | 133 |
| 10 | 40 | . 35 | 16 | . 37 | 2400 | 45 | - 61 |
| 11 | 44 | . 38 | 14 | . 43 | 2505 | 83 | 50 |
| 12 | 41 | . 41 | 15 | . 35 | 2465 | 67 | 58 |



D2 - Regression Equations for Individual Joints

```
TABLE D2.1. K-Factor Regression Equations and Corresponding R-Square Values for 3 Stringer Single-Faced
            Pallets
                        K-Factor Equations (1)R-Square
```

$K s 31=5.68635132-0.00002889(V)-0.00009837\left(L^{3}\right)-0.00000072(E)+0.17502467(I)$

$$
-0.39947025(W)-0.79014411(D)-0.00018179(M)
$$ ..... 0.738

```
ks32=5.66669504-0.00002389(V)-0.00010992(L3)-0.00000067(E)-0.41079192(W)}0.84
    -0.77619802(D) - 0.00014175(M)
0.762
Ks33 = 250.7705817-0.0008093(V) + 0.0000383(E) - 16.4948666(I) - 55.7927888(W)
(1) Symbol Definition:
L. = clear span distance between stringers
\(V=\) unit load
\(\mathrm{E}=\mathrm{MOE}\) of top deckboards
= moment of inertia of top deckboards combined
l = moment of inertia of top de
\(D=\) stringer height
\(M=\) average total Mmax along one stringer
```

TABLE D2.2. K-Factor Regression Equations and Corresponding R-Square Values for 3 Stringer Double-Faced Pallets

| K-Factor Equations (1) | R-Squa re |  |
| :---: | :---: | :---: |
| $\begin{aligned} K s 31= & 2.43228515-0.00006528\left(L^{3}\right)-0.0000011(E)+0.7814489(1)-0.21001454(W) \\ & -0.00004962(M) \end{aligned}$ | 0.783 |  |
| $\begin{aligned} K s 32= & 61.24254207+0.00172063(V)-0.00067536\left(L^{3}\right)-0.0000115(E)+1.37425331(1) \\ & -11.73232568(W)-9.31846199(D)+0.00115825(M) \end{aligned}$ | 0.702 |  |
| $\begin{aligned} K s 33 & =4.07106448-0.00008382\left(L^{3}\right)-0.00000046(E)+0.33723721(I)-0.89071147(W) \\ & -0.29950822(D)-0.00005554(M) \end{aligned}$ | 0.212 |  |
| $\begin{aligned} K s 34= & -5.93345235+0.00001408(V)+0.00009903\left(L^{3}\right)+0.00000148(E)-1.06035888(I) \\ & +1.06580506(W)+0.40450276(D)+0.00009852(M) \end{aligned}$ | 0.656 |  |
| $\begin{aligned} K s 35= & 197.9453275-0.0011024(V)-0.0005403\left(L^{3}\right)-0.0000144(E)+14.4007571(I) \\ & -19.5586775(W)-39.9635269(D)-0.0031941(M) \end{aligned}$ | 0.693 | N |
| $\begin{aligned} K s 36= & -2.61288313+0.00004959\left(L^{3}\right)+0.00000035(E)-0.26715823(I)+0.5579279(W) \\ & +0.19528509(D)+0.00004583(M) \end{aligned}$ | 0.060 |  |
| (1) Symbol Definition: |  |  |
| $L=$ clear span distance between stringers |  |  |
| $V=$ unit load |  |  |
| $E=$ MOE of top deckboards |  |  |
| 1 = moment of inertia of top deckboards combined <br> $W$ = average width of stringers |  |  |
| 0 ) stringer height |  |  |
| $M=$ average total Mmax along one stringer |  |  |


| TABLE D2.3. K-Factor Regression Equations and Corresponding R-Square Values for 4 St Pallets | Single-Faced |
| :---: | :---: |
| K-Factor Equations (1) | R-Square |
| $\begin{aligned} K s 41= & 5.0032253-1.20504034(D)-0.52384469(W)-0.00196144\left(L^{3}\right)+0.00000022(E)(I) \\ & -0.00035932(M) \end{aligned}$ | 0.953 |
| $\begin{aligned} K s 42= & 15.10242161-3.14771579(D)-2.50884051(W)+0.00184796\left(L^{3}\right)-0.00000036(E)(I) \\ & -0.00042289(M) \end{aligned}$ | 0.904 |
| $\begin{aligned} K s 43= & 10.5117218-2.32754501(D)-1.20354758(W)+0.00167631\left(L^{3}\right)+0.00000022(E)(1) \\ & -0.00058701(M) \end{aligned}$ | 0.935 |
| $\begin{aligned} K s 44= & -80.50777616+14.71527213(D)+22.43734744(W)+0.00105292\left(L^{3}\right) \\ & -0.00000017(E)(i)-0.0013589(M) \end{aligned}$ | 0.748 |
| (1) Symbol Definition: |  |
| $L$ = clear span distance between the outer and its adjacent stringer $V=$ unit load |  |
| $E=$ MOE of top deckboards |  |
| 1 = moment of inertia of top deckboards combined |  |
| $W=$ average width of stringers |  |
| $D=$ stringer height |  |
| $M=$ average total Mmax along one stringer |  |

TABLE D2.4. K-Factor Regression Equations and Corresponding R-Square Values for 4 Stringer Double-Faced Pallets

| K-Factor Equations (1) | R-Square |
| :---: | :---: |
| $K s 41=1.4137509-0.32359308(D)-0.6602909(W)+0.00221648\left(L^{3}\right)-0.00004882(M)$ | 0.782 |
| $K s 42=0.44967133-0.0006568(V)-5.41929666(D)+0.04637274\left(L^{3}\right)+0.00000912(E)(1)$ | 0.302 |
| $\begin{aligned} K s 43= & -1.14055642-0.0000537(V)+0.35941114(W)-0.00156753\left(L^{5}\right)+0.00000023(E)(I) \\ & -0.00001479(M) \end{aligned}$ | 0.780 |
| $\begin{aligned} K s 44= & -2.86183775+0.3980167(D)+1.07234489(W)-0.00086422\left(L^{3}\right)-0.0000006(E)(I) \\ & +0.00006394(M) \end{aligned}$ | 0.320 |
| $\begin{aligned} K s 45= & -2.51106256+0.30114723(D)+1.37424857(W)-0.00170584\left(L^{3}\right)-0.00000013(E)(I) \\ & +0.00009622(M) \end{aligned}$ | 0.693 |
| $K s 46=-16.50237272+0.0001487(V)+5.72319906(W)+0.01554779\left(L^{3}\right)+0.00000271(E)(1)$ | 0.584 |
| $\begin{aligned} K s 47= & 32.96264373-8.50611181(D)-2.76068946(W)+0.00224858\left(L^{3}\right)+0.00000028(E)(I) \\ & -0.00056211(M) \end{aligned}$ | 0.732 |
| $\begin{aligned} K s 48 & =4.55671798-0.93221829(D)-1.05516907(W)+0.00140221\left(L^{3}\right)+0.0000007(E)(I) \\ & -0.0001293(M) \end{aligned}$ | 0.486 |
| (1) Symbol Definition: |  |
| $\begin{aligned} & L=c l e a r \text { span distance between the outer and its adjacent stringer } \\ & \underline{V}=\text { unit load } \end{aligned}$ |  |
| $E=$ MOE of top deckboards |  |
| 1 = moment of inertia of top deckboards combined |  |
| $W=$ average width of stringers |  |
| $\mathrm{J}=$ stringer height |  |
| $M=$ average total Mmax along one stringer |  |

$L=c l e a r$ span distance between the outer and its adjacent stringer
$V=$ ullit load
$E=$ MOE of top deckboards
rtia of top deckboards combi
I = stringer height
$M=$ average total Mmax along one stringer

The vita has been removed from the scanned document


[^0]:    ${ }^{1}$ Characteristics given are

    1. $M_{\max }$ (in.-lb.)
    2. R (in.-lb./radian)
